



**3° C.F.P.B.**  
3º CONGRESO - SEMINARIO INTERNACIONAL  
DE FUNDACIONES PROFUNDAS  
DEL 27 AL 29 DE ABRIL DE 2017



# DESIGN OPTIONS FOR PILED RAFTS AN OVERVIEW



UNIVERSITÀ DEGLI STUDI DELLA CAMPANIA  
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SCUOLA POLITECNICA E DELLE SCIENZE DI BASE

DIPARTIMENTO DI INGEGNERIA CIVILE  
DESIGN EDILIZIA E AMBIENTE

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**Head of the Department**

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Scientific understanding proceeds by way of constructing and analysing **models** of the segments or aspects of reality under study. The purpose of these models **is not to give a mirror image** of reality, not to include all its elements in their exact sizes and proportions, but **rather to single out** and make available for intensive investigation **those elements which are decisive.**



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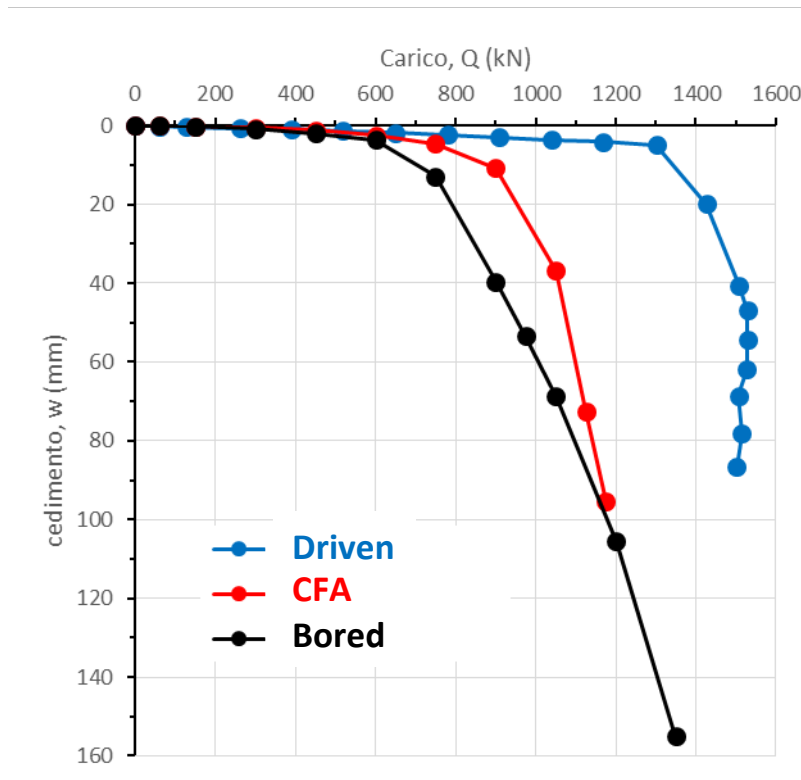
BARAN P.A., SWEEZY P.M. (1968)

*Monopoly Capital: an essay on the American economic and social order.*



# The role played by pile technology .....

## International Prediction Event – Portugal, ISC 2002

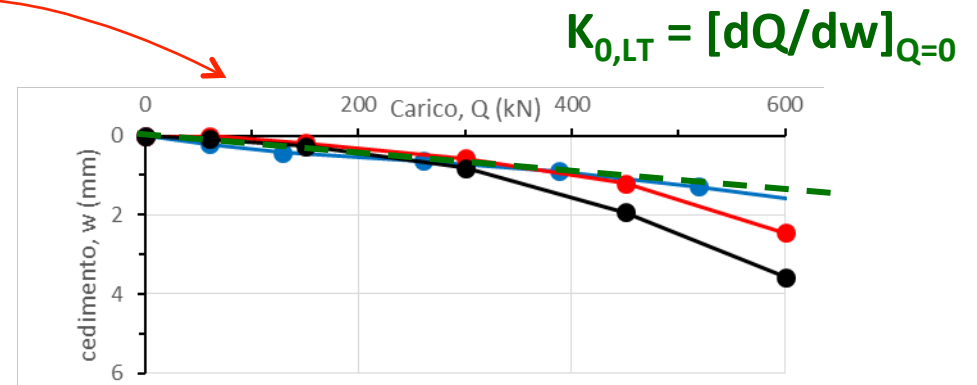
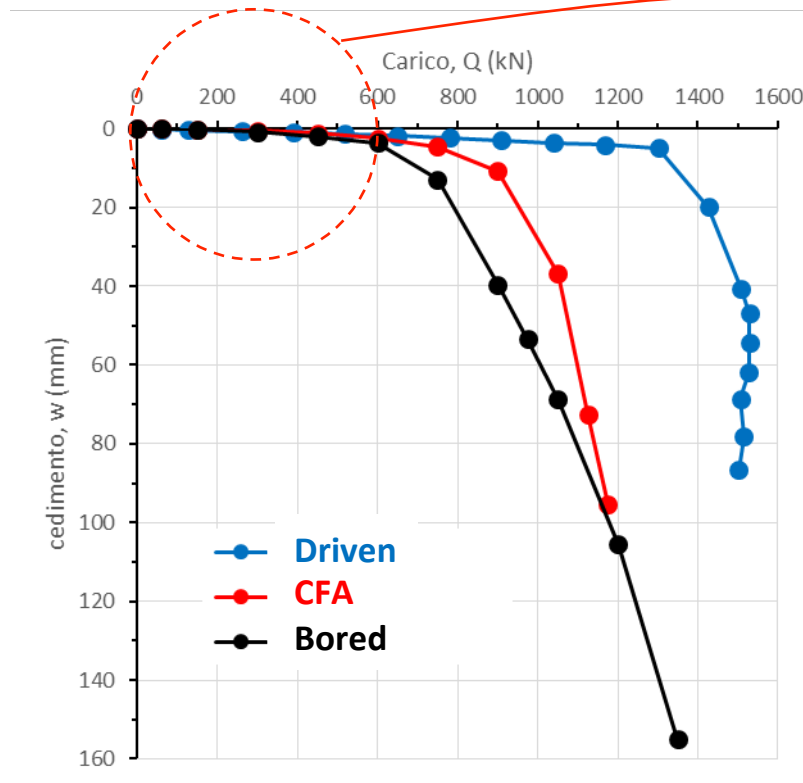


The shape of the curves are different pile by pile



# The role played by pile technology .....

## International Prediction Event – Portugal, ISC 2002



The initial tangent is almost the same for any pile



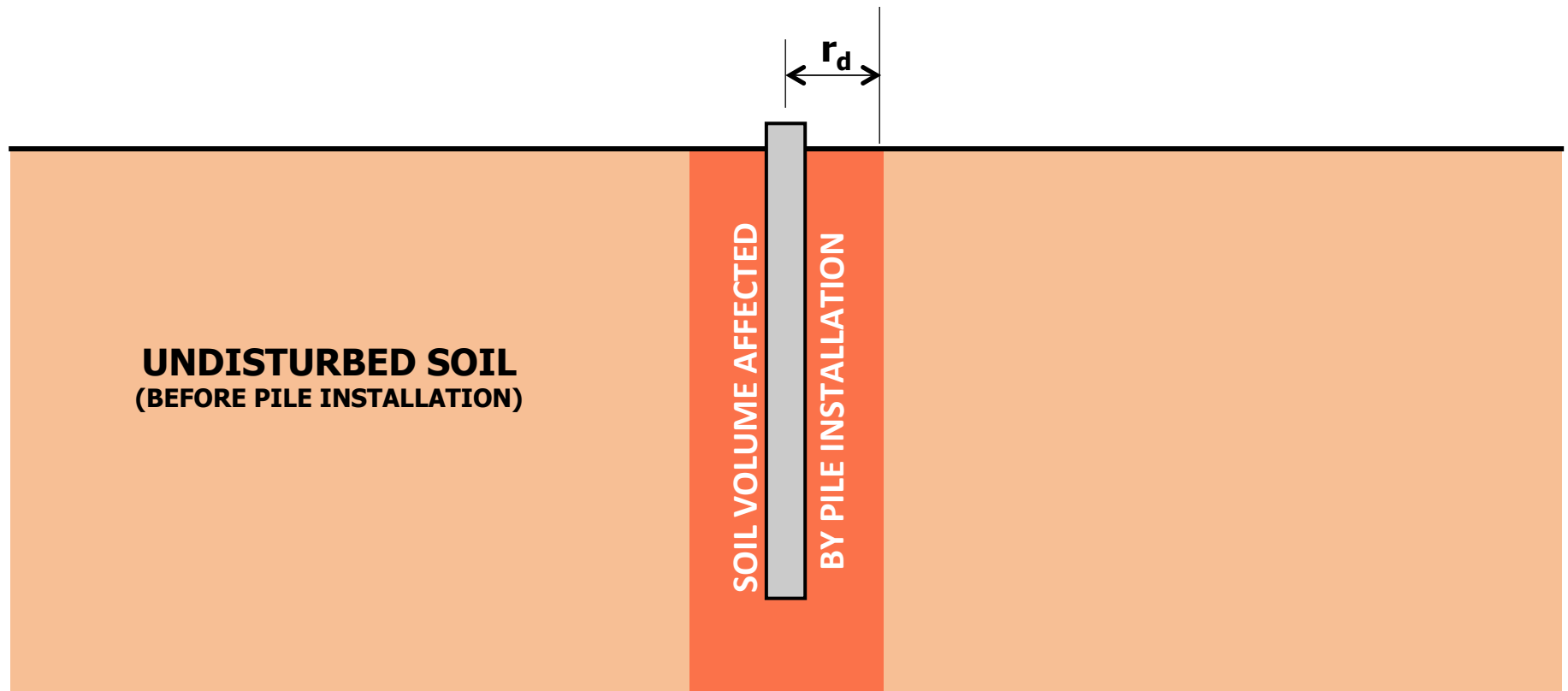


# SIMPLE EXPLANATION

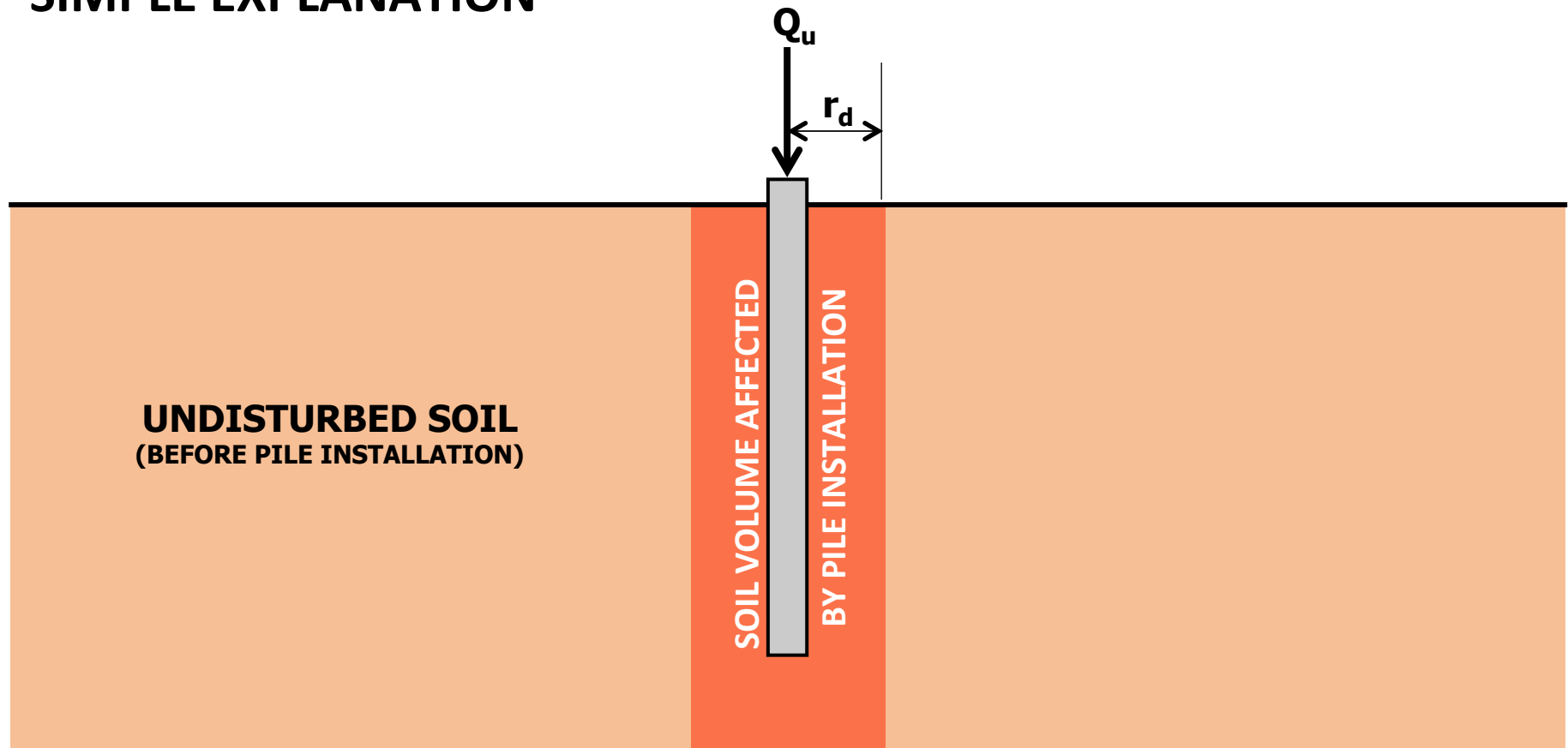
**UNDISTURBED SOIL  
(BEFORE PILE INSTALLATION)**



# SIMPLE EXPLANATION



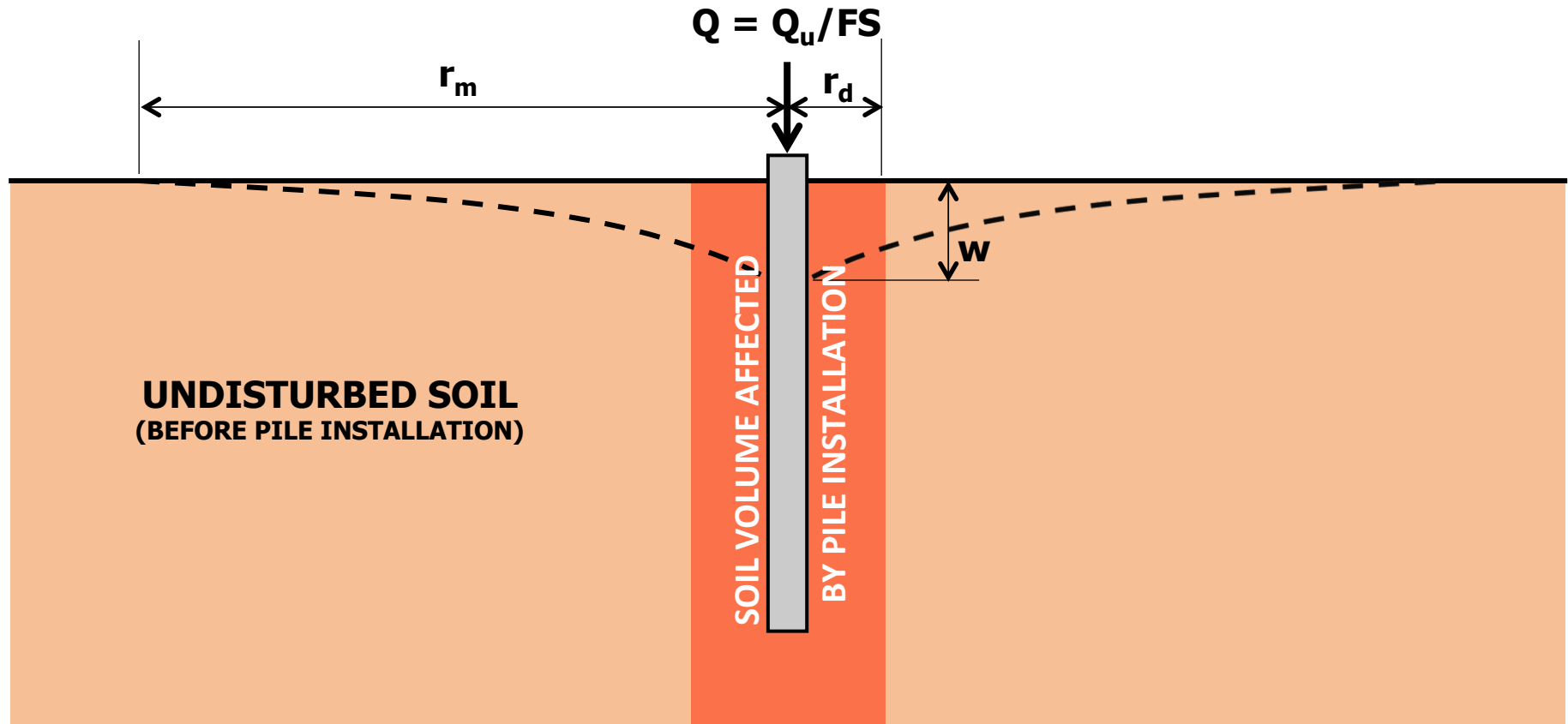
## SIMPLE EXPLANATION



**Failure develops in a thin soil cylinder within the affected one → great influence of the specific installation procedure**



## SIMPLE EXPLANATION



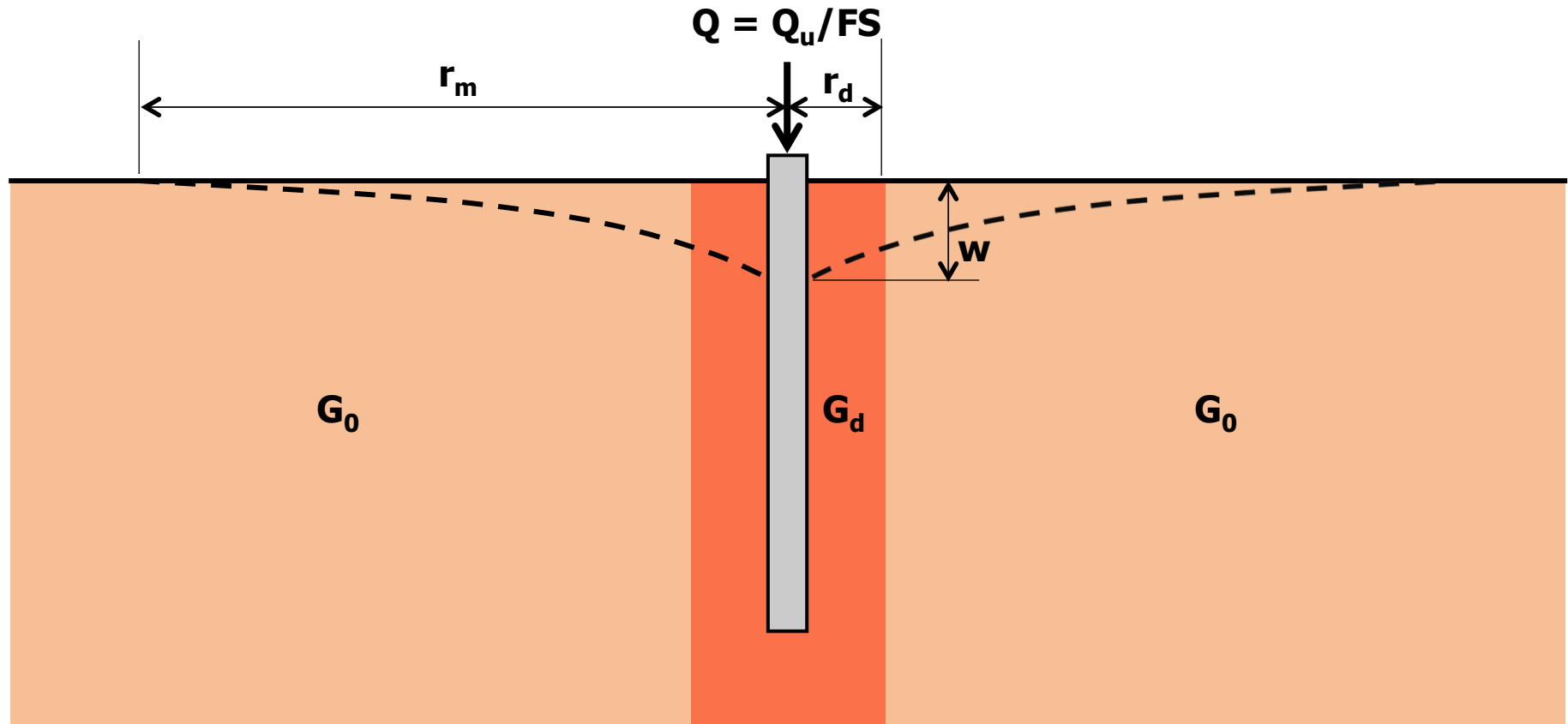
$$r \downarrow m = 2.5 \cdot (1 - \nu) \cdot L = (1.25 \div 2.50) \cdot L$$

$$r \downarrow d = (1.25 \div 2.5) \cdot d$$

$$r \downarrow m / r \downarrow d = (0.5 \div 2) \cdot L / d \gg \gg 1$$



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# **ELASTIC THEORY, ALBEIT NOT ADEQUATE FOR PROBLEMS INVOLVING SOIL, IS A VERY SIMPLE TOOL TO DETECT MAIN ASPECTS**



## A simple formula for evaluating axial soil-pile stiffness $K_0$

Fleming et al., 2009: rigid pile embedded in an homogeneous elastic half-space

$$K_0 = 2 \cdot \pi \cdot G_0 \cdot L / \zeta$$

$$\zeta = \ln[5 \cdot (1 - \nu) \cdot L/d] \rightarrow \text{for usual } L/d \text{ and } \nu \quad 3 \leq \zeta \leq 5$$



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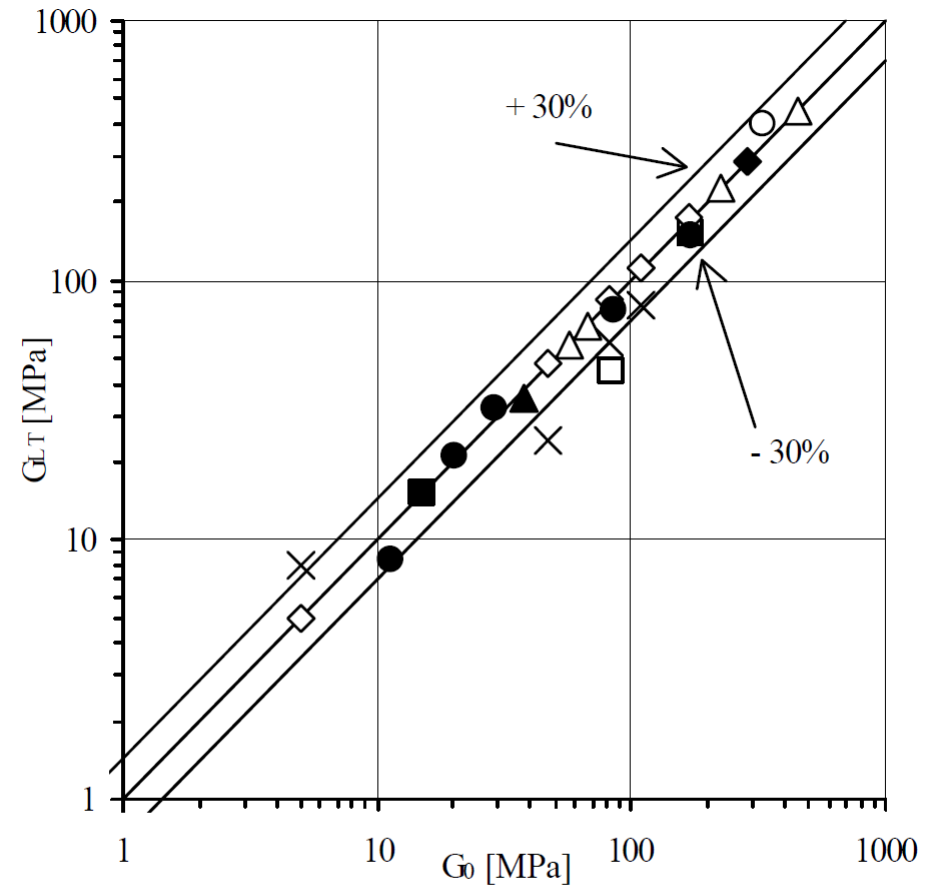
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$$K_{\downarrow 0} \sim 0.5 \cdot \pi \cdot G_{\downarrow 0} \cdot L$$

$$G_{\downarrow 0, LT} \sim 2 \cdot K_{\downarrow 0, LT} / \pi \cdot L$$



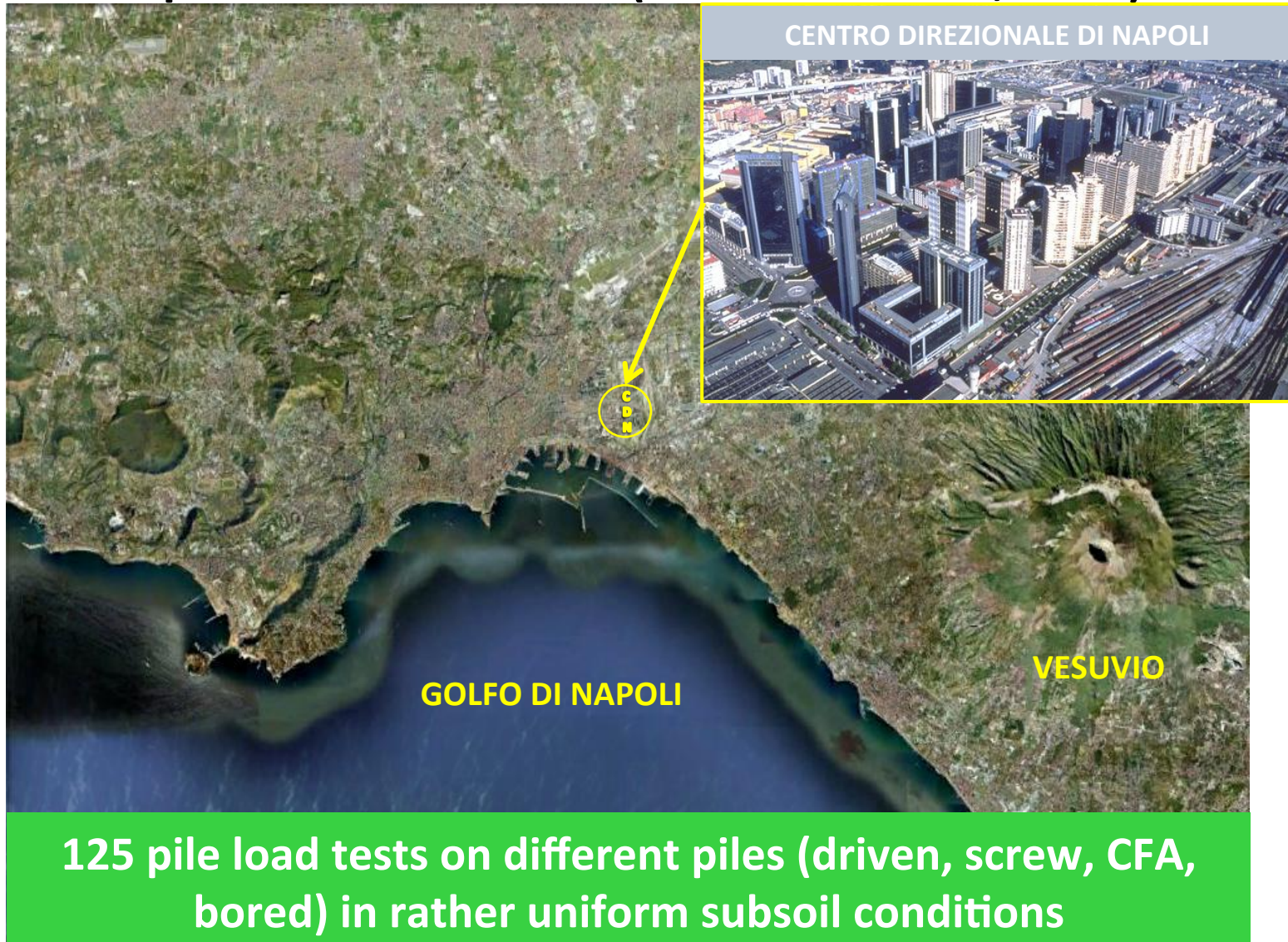
**Mandolini & Viggiani (1997):**  
***Settlement of piled foundations.***  
**Geotéchnique, vol. 47(4)**  
 Bishop Gold Medal Award by ICE, London, UK



- |                             |                               |
|-----------------------------|-------------------------------|
| ■ Cooke et al. (1980)       | ◆ O'Neill et al. (1982)       |
| ▲ Briaud et al. (1989)      | □ Viggiani (1989)             |
| ◇ Caputo et al. (1991)      | × Mandolini & Viggiani (1992) |
| ● Russo (1994)              | △ Rampello (1994)             |
| ○ Fioravante & Sarri (1997) |                               |



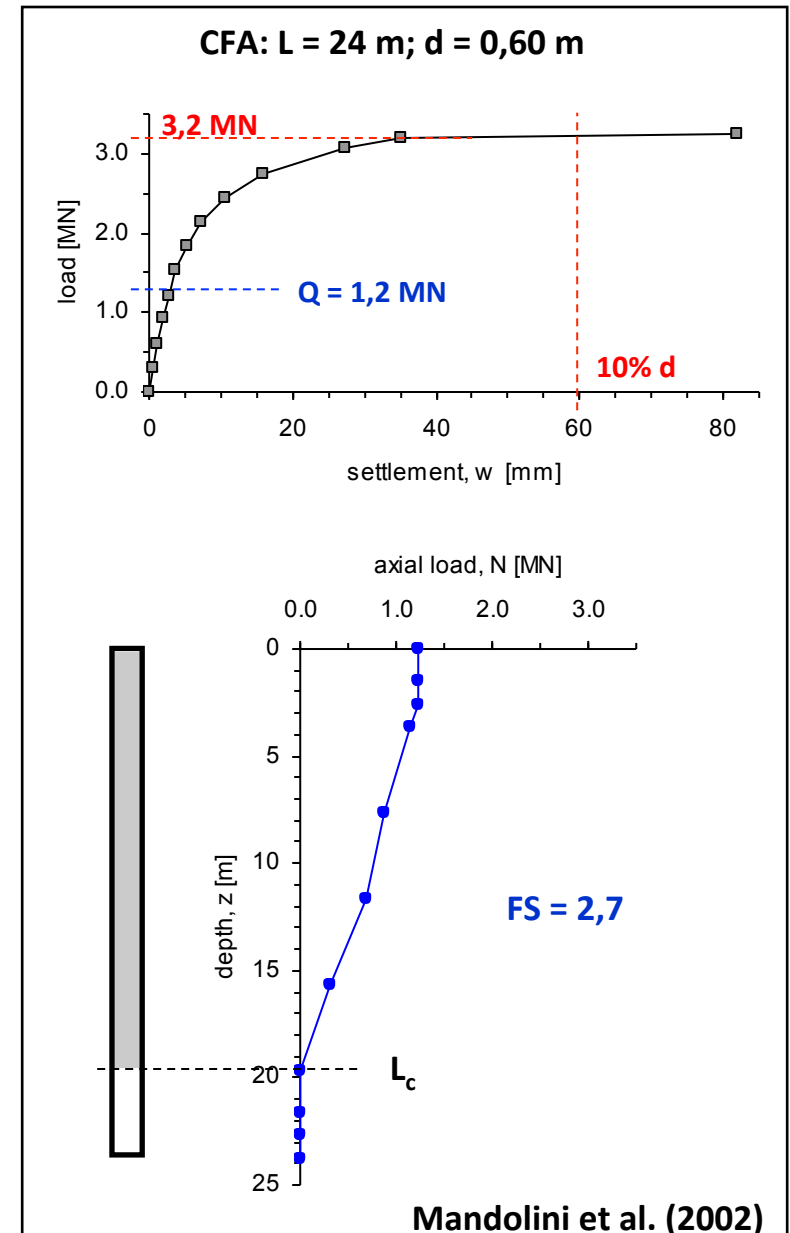
## Collected experimental evidence (Mandolini et al., 2005)



**125 pile load tests on different piles (driven, screw, CFA, bored) in rather uniform subsoil conditions**



$$L_c \sim 1.5 \cdot (E_p / G)^{0.5}$$



## Collected experimental evidence (Mandolini et al., 2005)

$d = 0.35 \div 2.00 \text{ m}$

$L = 9.5 \div 42.0 \text{ m}$

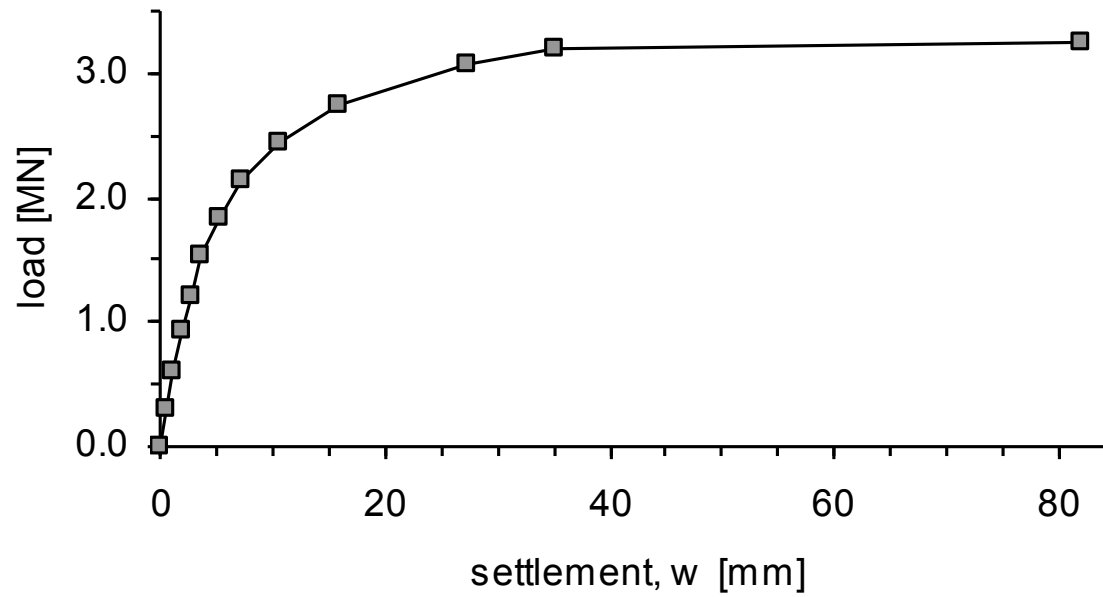
$L/d = 16 \div 61$

$$RS_{\downarrow av} = K_{\downarrow 0, meas.} / (EA/L_{\downarrow c})$$

Pile type	$(RS)_{av}$	COV(RS)
Bored	1,46 (1)	0,28
CFA	1,44 ( $\approx 1$ )	0,46
Displacement	1,29 ( $\approx 0.9$ )	0,42

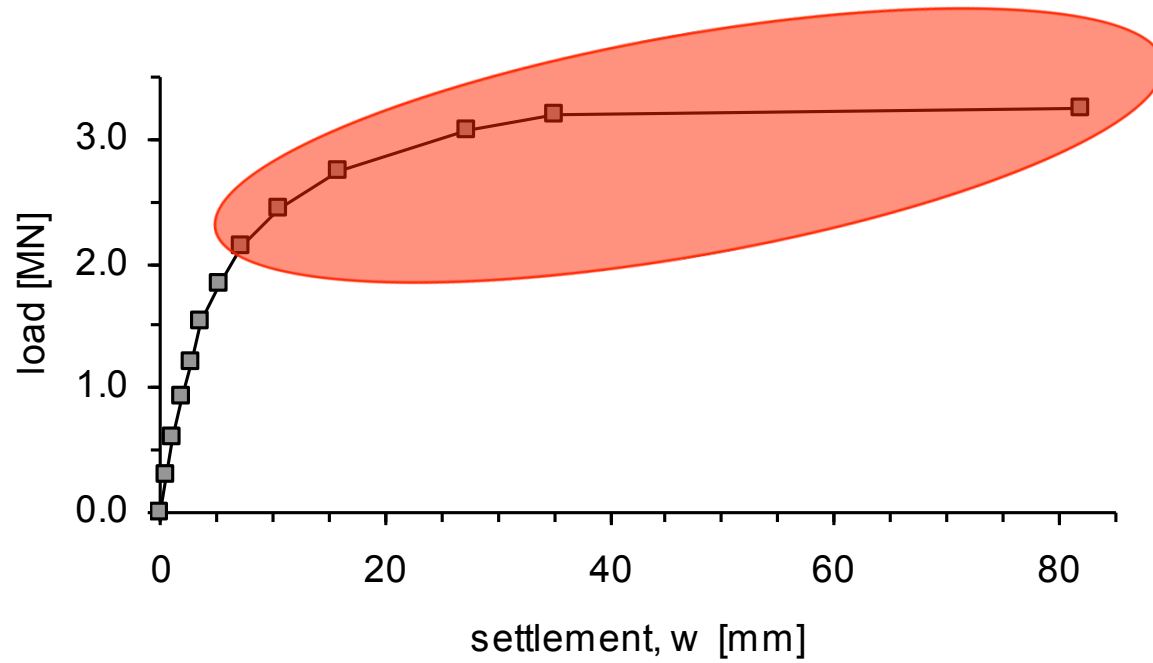


## Summarizing:



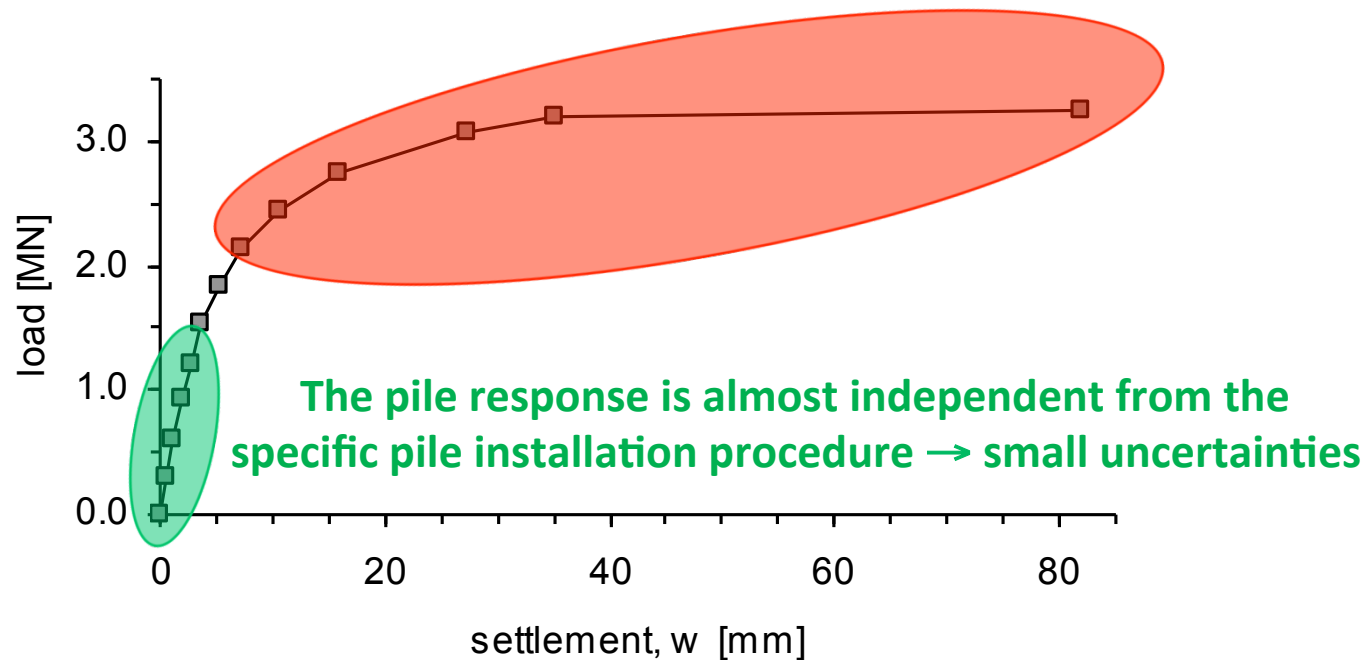
## Summarizing:

The pile response depends on the soil changes due to the specific pile installation procedure → great uncertainties



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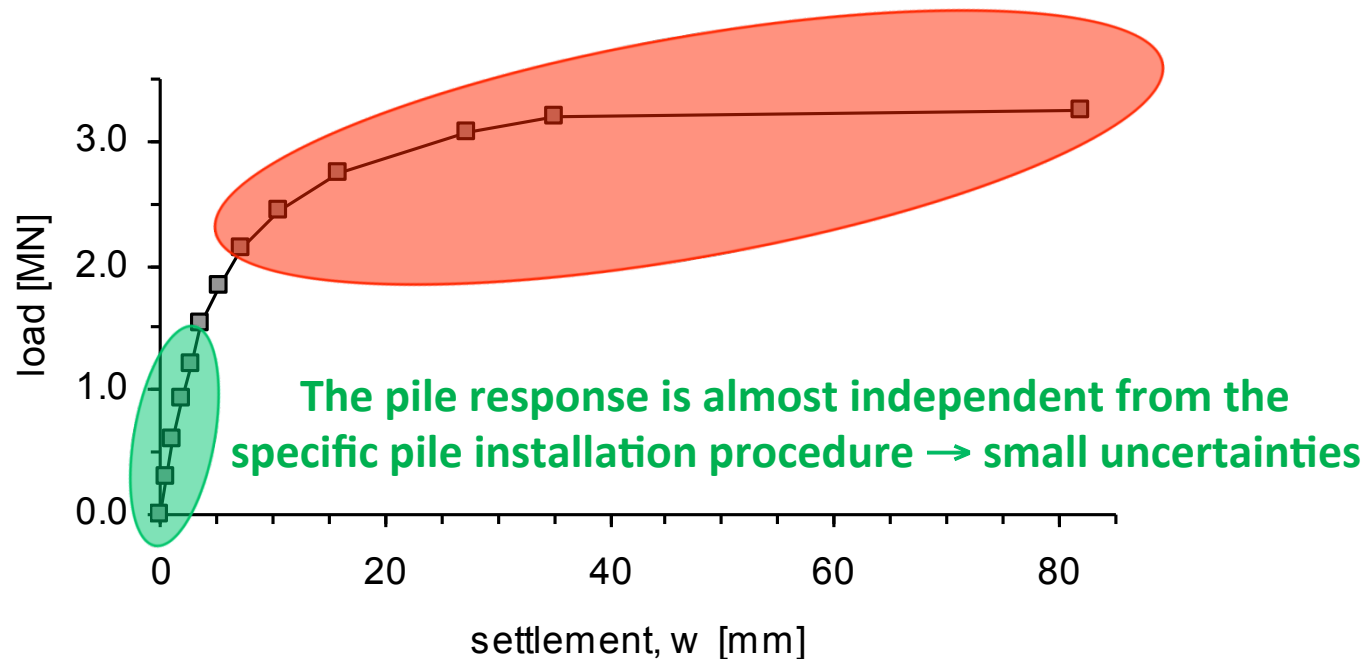
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## Summarizing:

The pile response depends on the soil changes due to the specific pile installation procedure → great uncertainties



When dealing with piles, the more reliable design method is that of minimizing sensitivity to pile technology → **stiffness and not capacity !!!**



**The only way to hopefully give a good answer is that of having a good question:**

# **WHY PILES ARE NEEDED ?**



# **ELASTIC THEORY, ALBEIT NOT ADEQUATE FOR PROBLEMS INVOLVING SOIL, IS A VERY SIMPLE TOOL TO DETECT MAIN ASPECTS**



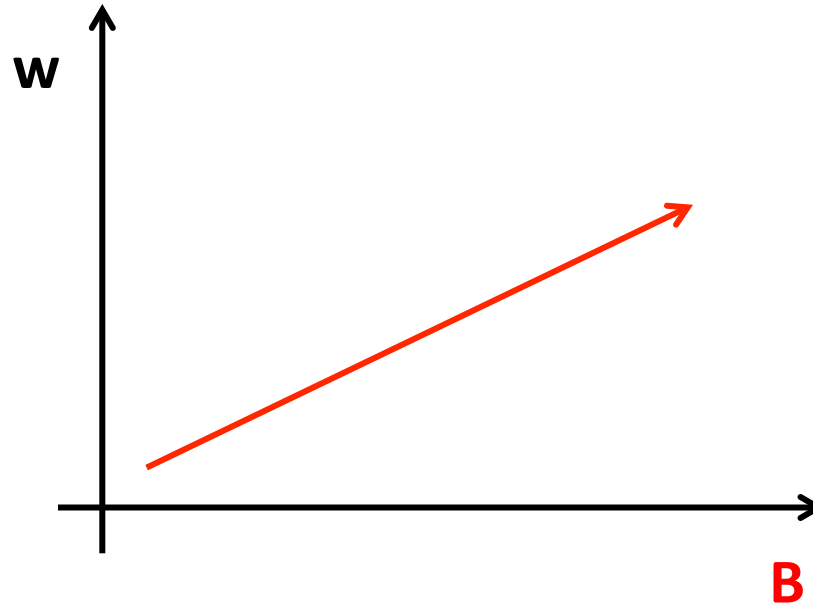
## Average settlement of shallow foundation:

$$w = q \cdot B / E \cdot I = q_{lim} \cdot B / FS \cdot E \cdot I$$



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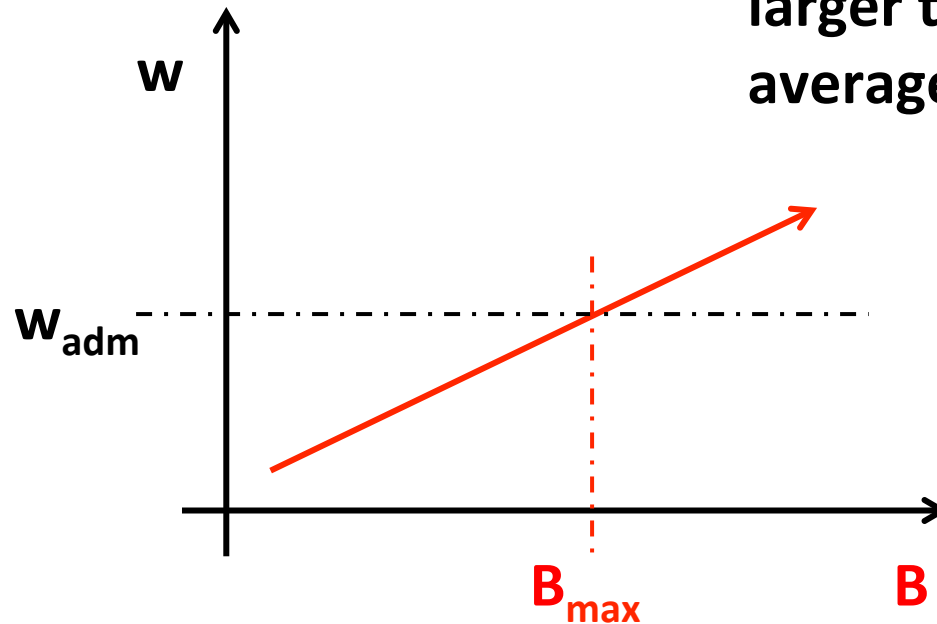
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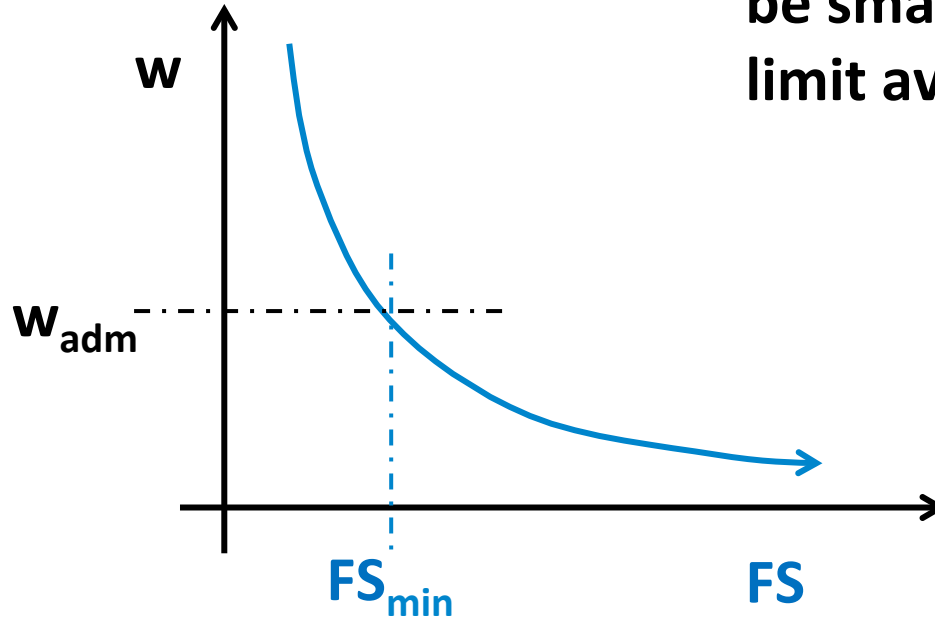
For a given soil stiffness and FS, foundation width should not be larger than **B<sub>max</sub>** in order to limit average settlement.



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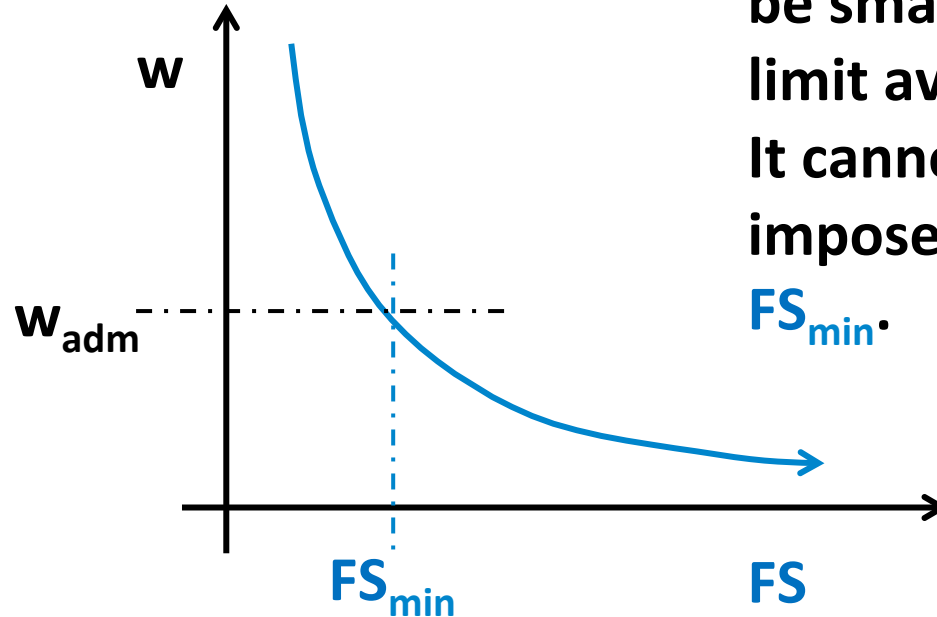
$$w = q \cdot B / E \cdot I = q_{lim} \cdot B / FS \cdot E \cdot I$$

For a given soil stiffness and foundation width, FS should not be smaller than  $FS_{min}$  in order to limit average settlement.



## Average settlement of shallow foundation:

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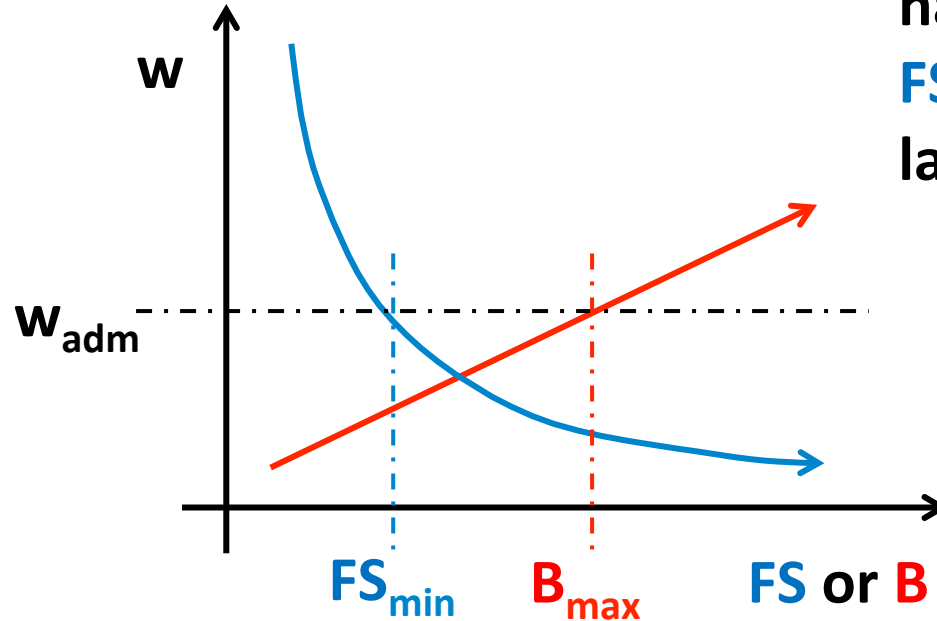
For a given soil stiffness and foundation width,  $FS$  should not be smaller than  $FS_{min}$  in order to limit average settlement. It cannot be said that  $FS$  as imposed by Codes is larger  $FS_{min}$ .





## Average settlement of shallow foundation:

$$w = q \cdot B / E \cdot I = q_{lim} \cdot B / FS \cdot E \cdot I$$



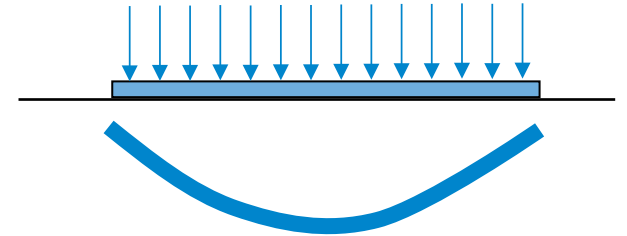
Large structures (**large B**) have typically larger  $FS$  ( $> FS_{min}$ ) but could suffer large average settlement.



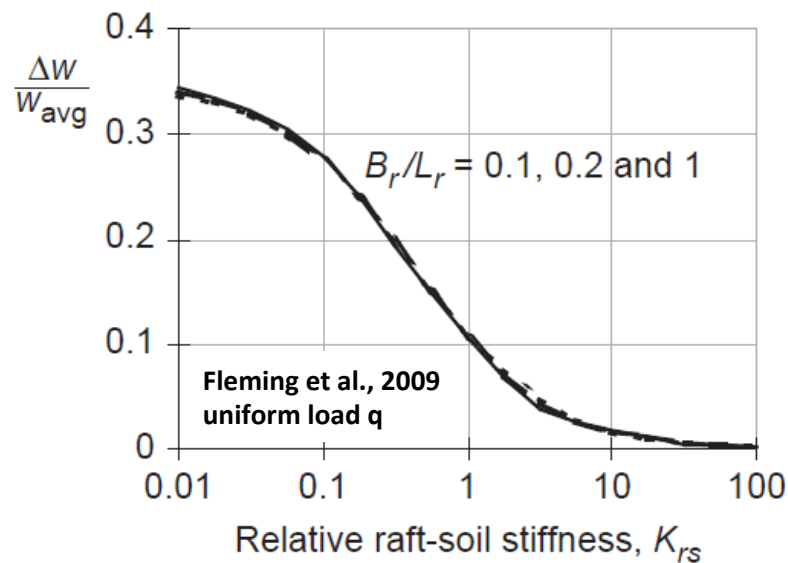
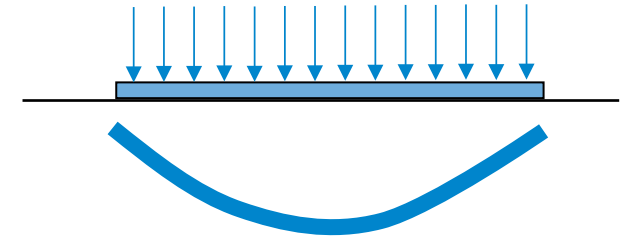
# 1. Piles can help in reducing average settlement



**Large rafts have necessarily small  
raft-soil relative stiffness  $K_{rs}$   
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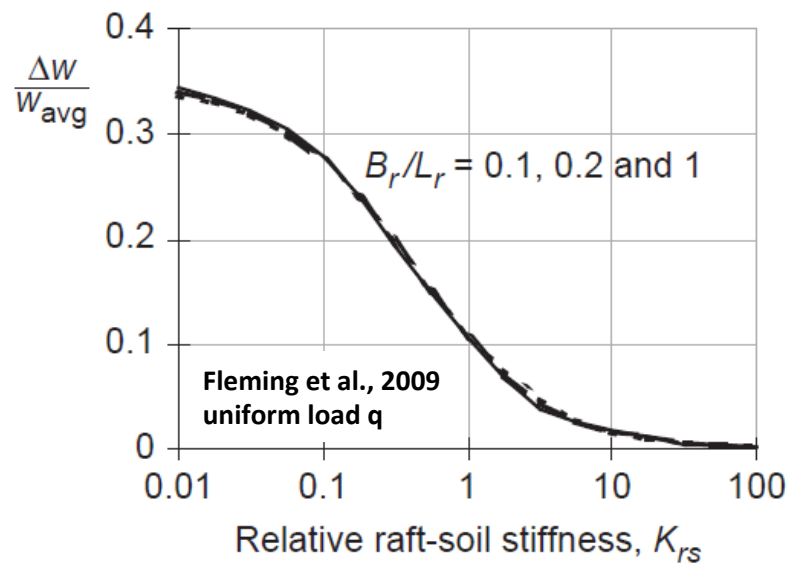
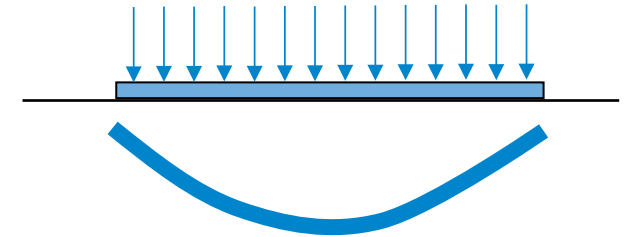


**For small values of  $K_{rs}$ , expected differential settlement can be  $\sim 1/3$  of the expected average settlement of the unpiled raft (homogeneous soil conditions).**

$$K_{rs} = 5.57 \frac{E_r}{E_s} \frac{1 - \nu_s^2}{1 - \nu_r^2} \left( \frac{B_r}{L_r} \right)^{0.5} \left( \frac{t_r}{L_r} \right)^3$$



**Large rafts have necessarily small raft-soil relative stiffness  $K_{rs}$  (expected dishing).**

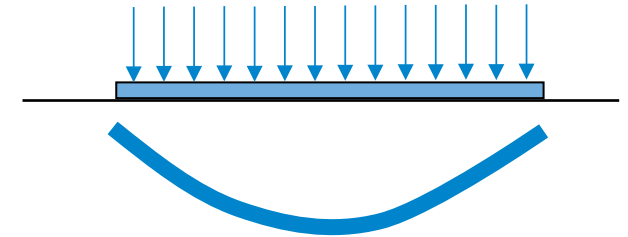


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**Clearly, the larger the raft is, the thicker it should be.**

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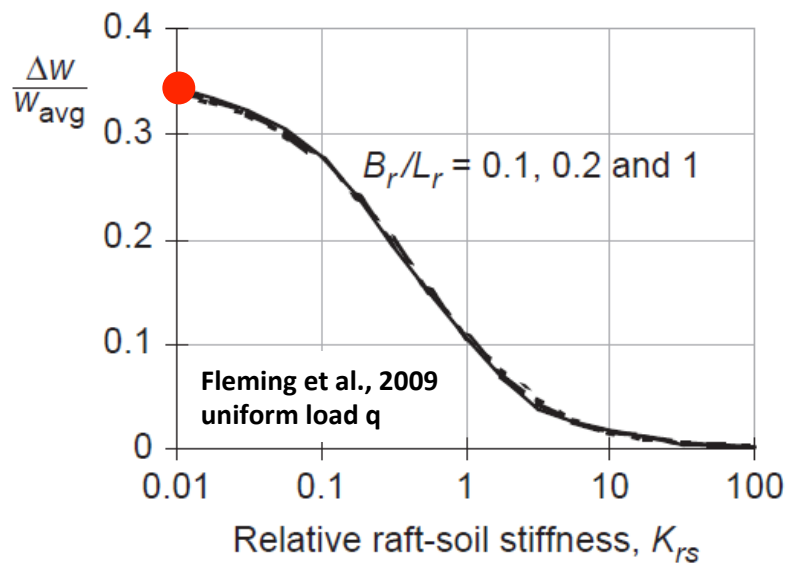
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### EXAMPLE

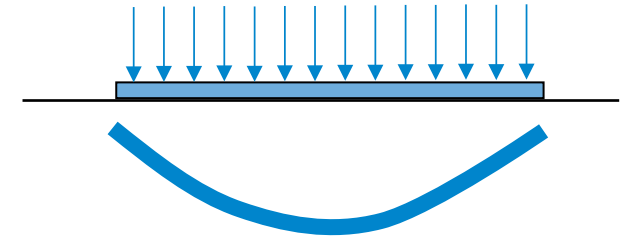
$B_r = 50 \text{ m}$ ;  $L_r = 50 \text{ m}$ ;  $E_r/E_s = 250$   
 $\nu_s = 0.30$ ;  $\nu_r = 0.15$

$\Delta w/w_{avg} = 0.33$  ( $K_{rs} = 0.01$ )  $\rightarrow$   
 $t_r \sim 1 \text{ m}$



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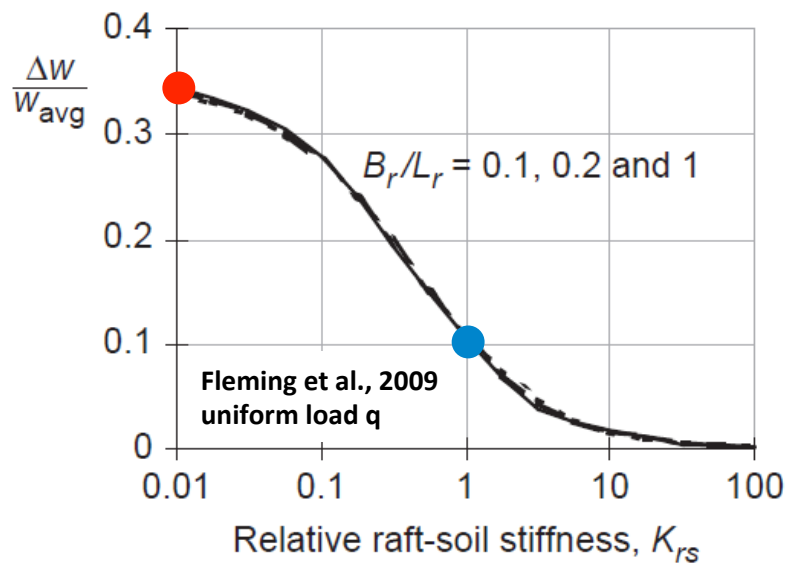


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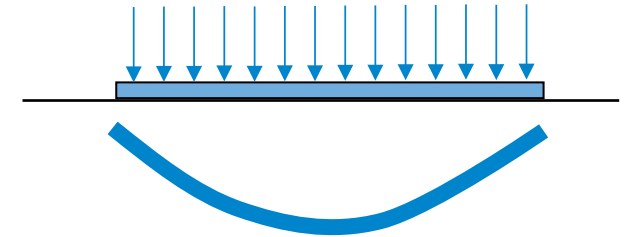
$\Delta w/w_{avg} = 0.33$  ( $K_{rs} = 0.01$ )  $\rightarrow$   
 $t_r \sim 1 \text{ m}$

$\Delta w/w_{avg} = 0.1$  ( $K_{rs} = 1$ )  $\rightarrow$   
 $t_r \sim 4.6 \text{ m}$



$$K_{rs} = 5.57 \frac{E_r}{E_s} \frac{1 - \nu_s^2}{1 - \nu_r^2} \left( \frac{B_r}{L_r} \right)^{0.5} \left( \frac{t_r}{L_r} \right)^3$$

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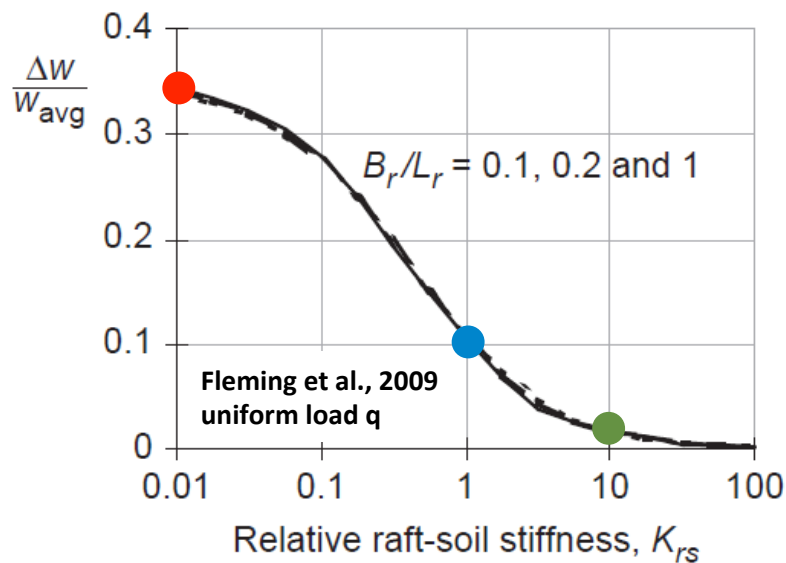
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 $t_r \sim 4.6 \text{ m}$

$\Delta w/w_{avg} \sim 0$  ( $K_{rs} = 10$ )  $\rightarrow$   
 $t_r \sim 9.9 \text{ m}$



$$K_{rs} = 5.57 \frac{E_r}{E_s} \frac{1 - \nu_s^2}{1 - \nu_r^2} \left( \frac{B_r}{L_r} \right)^{0.5} \left( \frac{t_r}{L_r} \right)^3$$



- 1. Piles can help in reducing average settlement**
- 2. Piles can help in reducing differential settlement**



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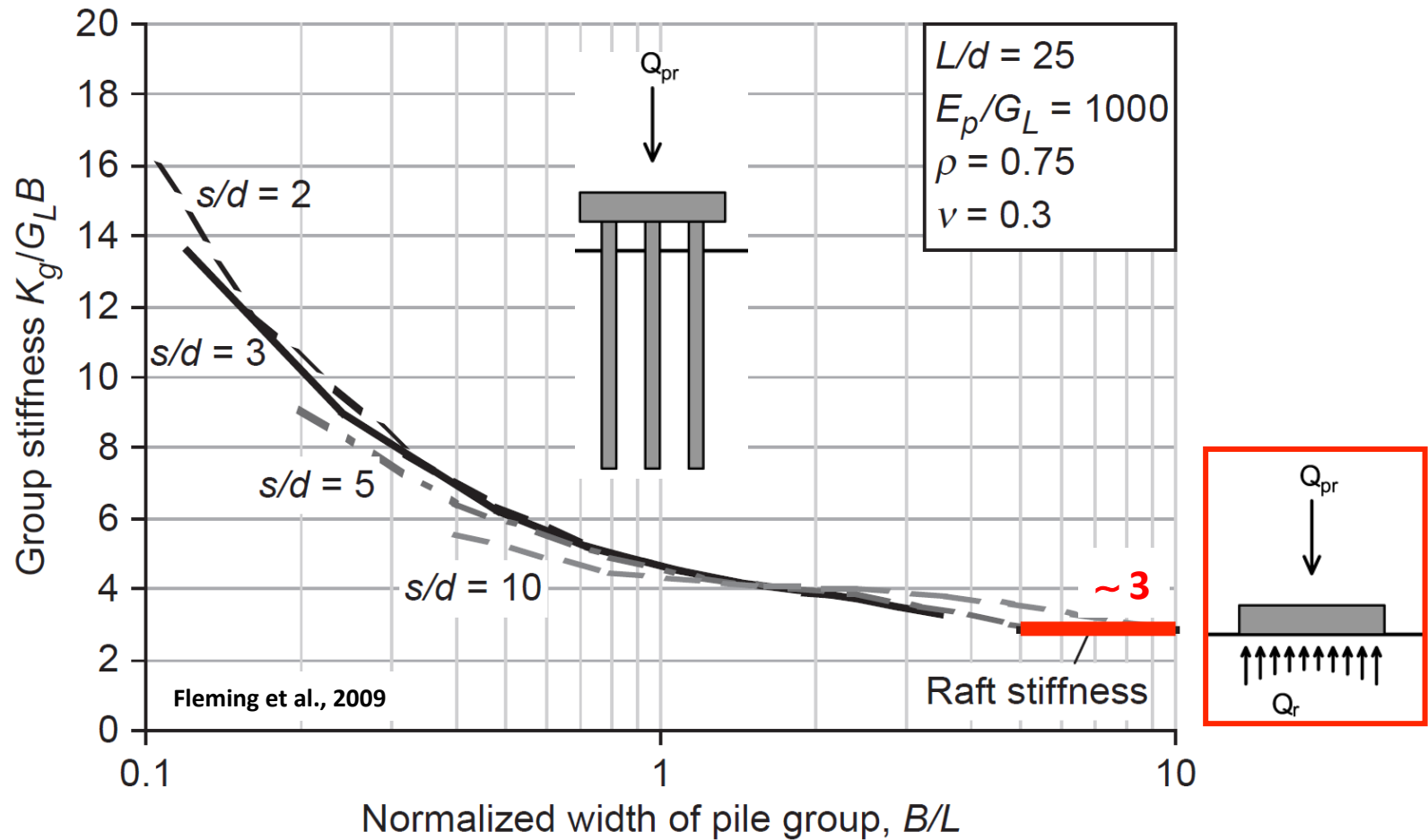
**IS IT TRUE ?**



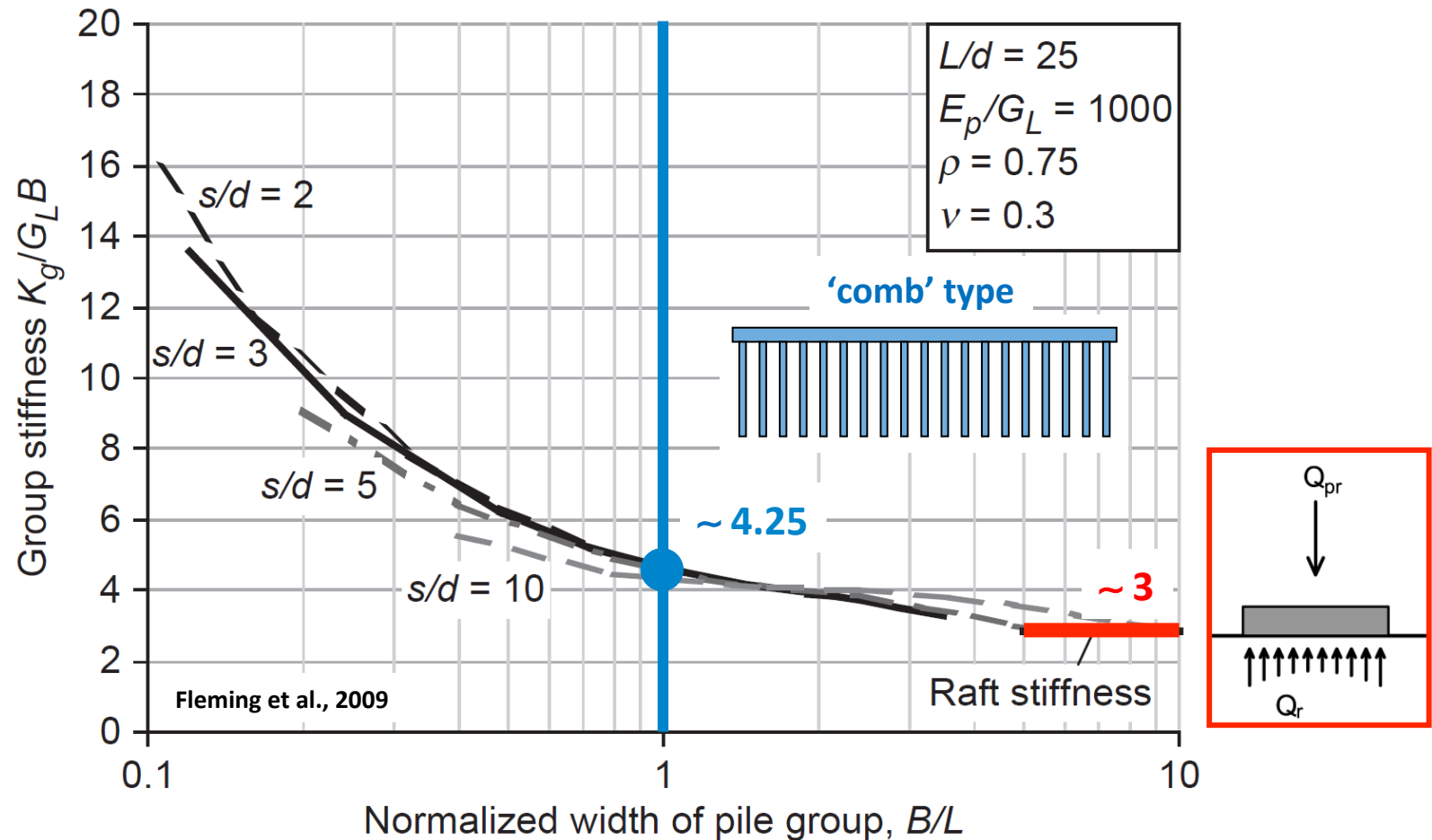
$$K \downarrow UR = 2 \cdot G \cdot B / I \cdot (1 - \nu) \rightarrow \text{square raft} \quad K \downarrow UR / G \cdot B = 2 / 0.946 \cdot (1 - 0.3) \sim 3$$



# Linear elastic solution for pile group stiffness



If the ratio  $B/L$  is large enough (say  $B/L > 1$ ), adding piles is not very effective in increasing stiffness ( $4.25/3 \sim 1.4$ ).



It is the case of large structures (large B): for practical pile length, it is often impossible to have  $B/L < 1$ .

### EXAMPLE

$B = 50 \text{ m}$

$L = 50 \text{ m}$

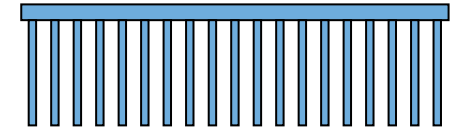
$d = 2 \text{ m}$

$s = 8 \text{ m (4d)}$

$N = 49 \text{ piles}$

$$K \downarrow G / G \cdot B = 4,25$$

'comb' type



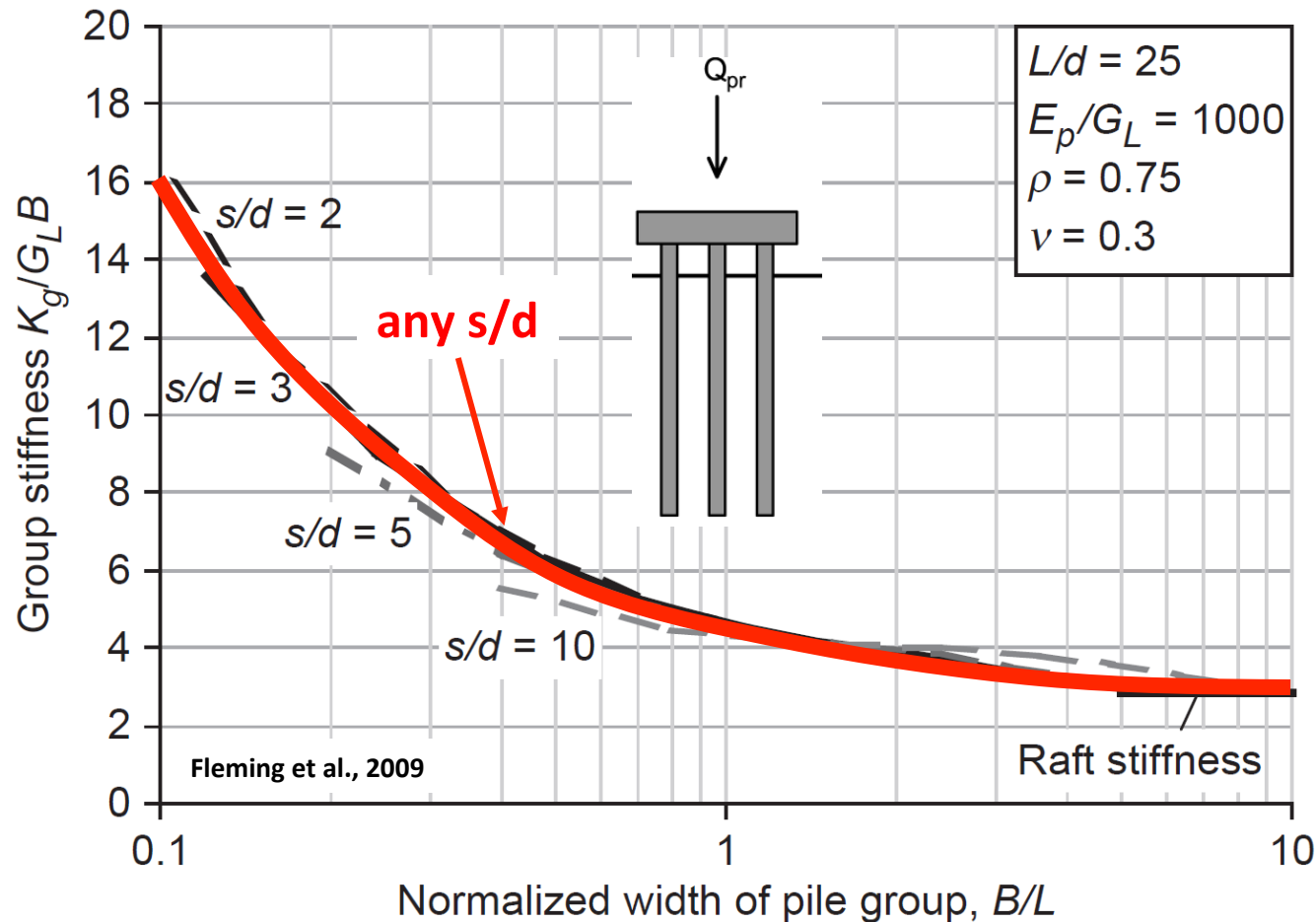
**49 large diameter piles**

**(~ 2500 m total length, ~ 8000 m<sup>3</sup> concrete and soil removal, steel)**

**to reduce average settlement by 40% !!!!!**



Due to the superimposition of curves for different spacing ratio  $s/d$ , the same pile group stiffness can be obtained with less but more spaced piles.



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### EXAMPLE

B = 50 m

L = 50 m

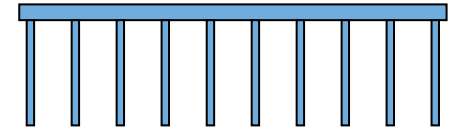
d = 2 m

s = 16 m (8d)

N = 16 piles

$$K \downarrow G / G \cdot B = 4,25$$

optimized 'comb' type

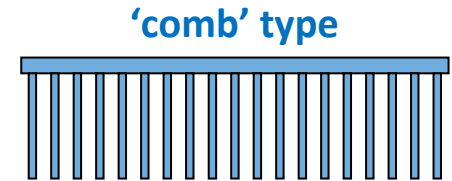


**16 large diameter piles, but more spaced,  
(~ 1/3 of the previous solution)  
have the same effects!!!!**



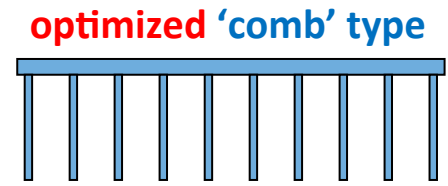
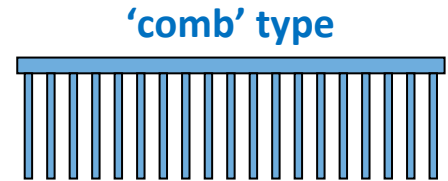


**Typically, a large raft has enough resistance;  
piles are hence needed only to reduce  
settlement.**

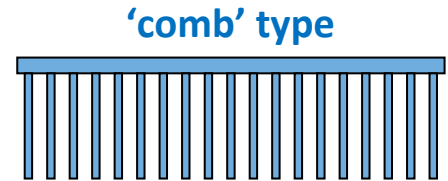


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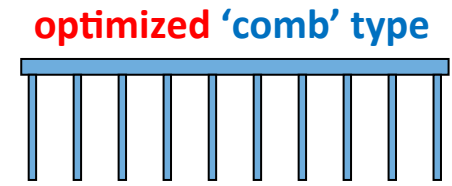
Due to practical problem, it is often impossible to have  $B/L < 1$ . In these cases, piles can only slightly reduce average settlement (up to 40% in relatively homogeneous soil conditions). **Optimized layouts should be pursued.**



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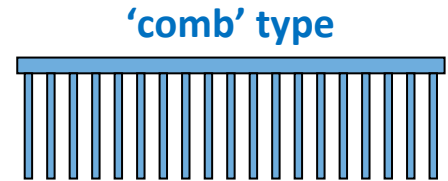


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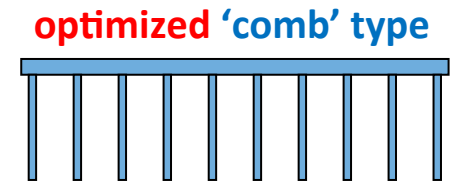


**WARNING: If a reduction of 40% is not enough, adding piles do not help to satisfy that design requirement for which they have been considered.**

Typically, a large raft has enough resistance; piles are hence needed only to reduce settlement.



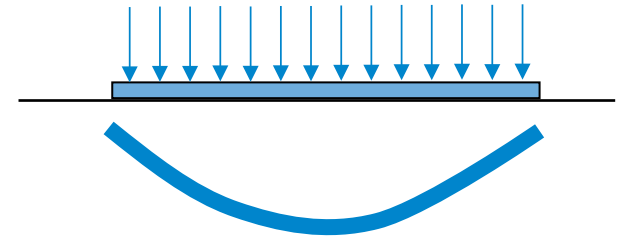
Due to practical problem, it is often impossible to have  $B/L < 1$ . In these cases, piles can only slightly reduce average settlement (up to 40% in relatively homogeneous soil conditions). **Optimized layouts should be pursued.**



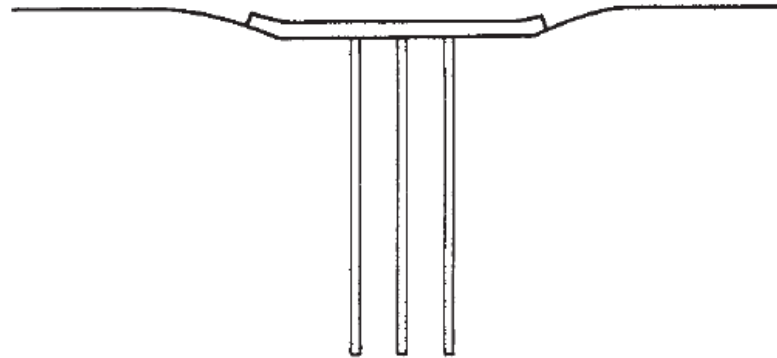
**WARNING:** If a reduction in settlement is not enough, adding more piles does not help to satisfy the design requirement for which they are considered.



# Piles strategically placed in order to reduce differential settlement.



(a) Dishing of unpiled raft



(b) Effect of differential settlement reducing piles



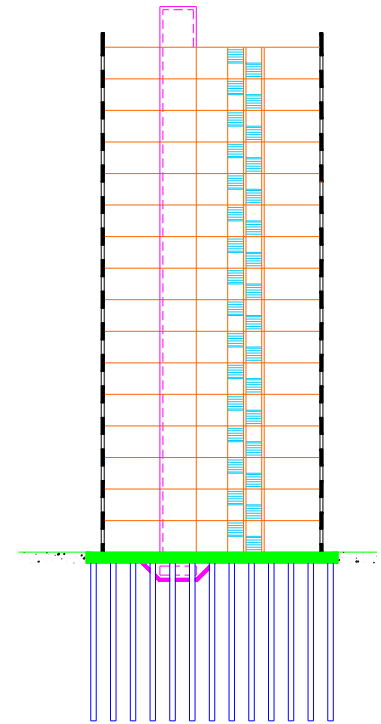
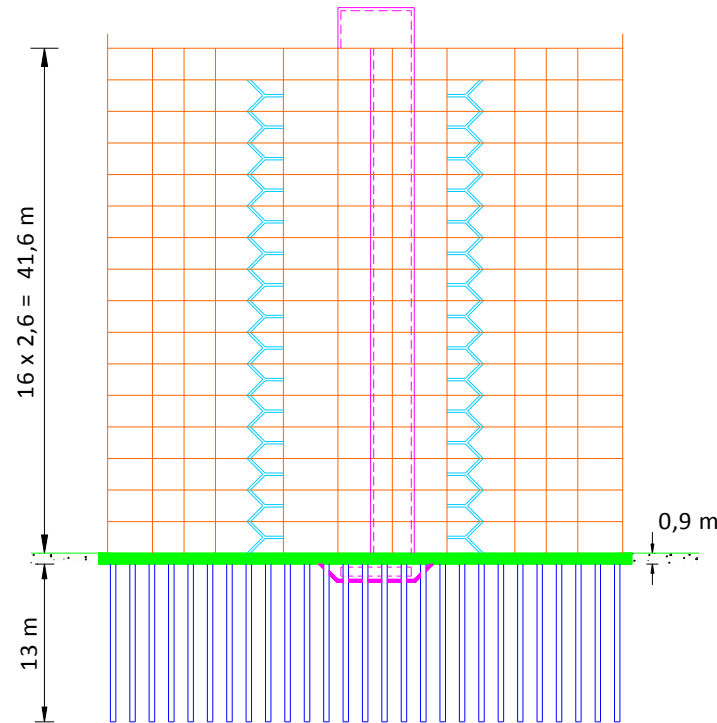
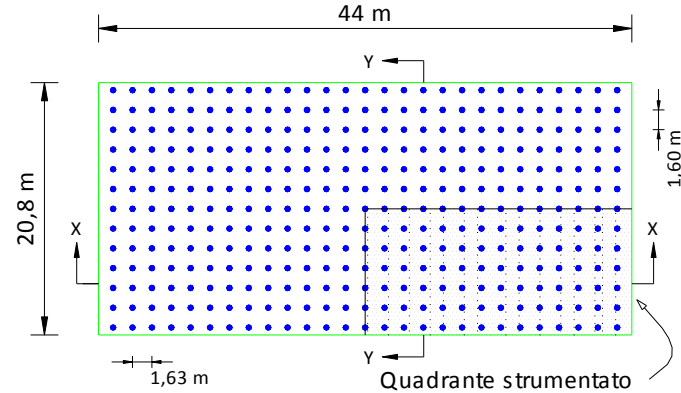
# STONEBRIDGE PARK BUILDING (Cooke et al., 1980)

London clay:

$c_u \sim 100 \text{ kPa}$

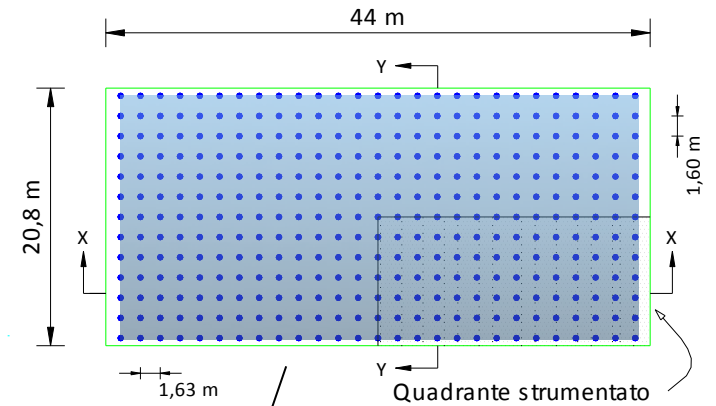
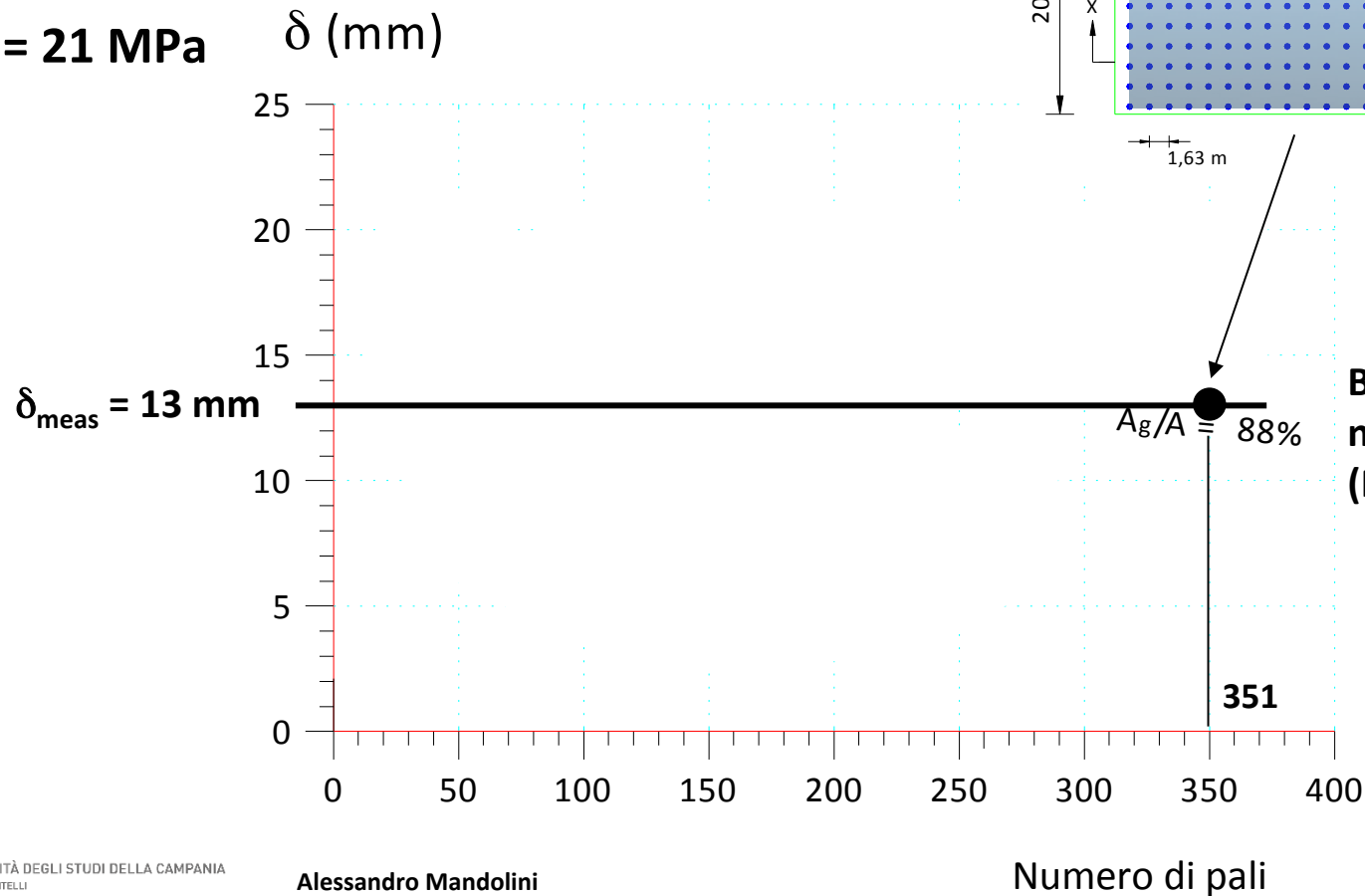
$G_0 = 21 \text{ MPa}$

Pianta della fondazione  
(351 pali;  $d = 450 \text{ mm}$ ;  $L = 13 \text{ m}$ )



# STONEBRIDGE PARK BUILDING (Cooke et al., 1980)

London clay:  
 $c_u \sim 100 \text{ kPa}$   
 $G_0 = 21 \text{ MPa}$

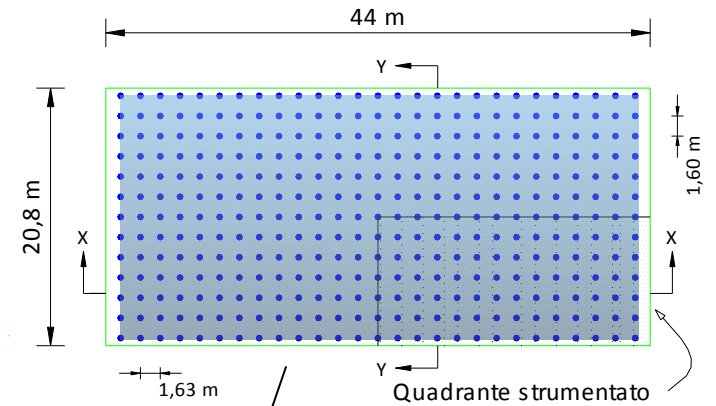
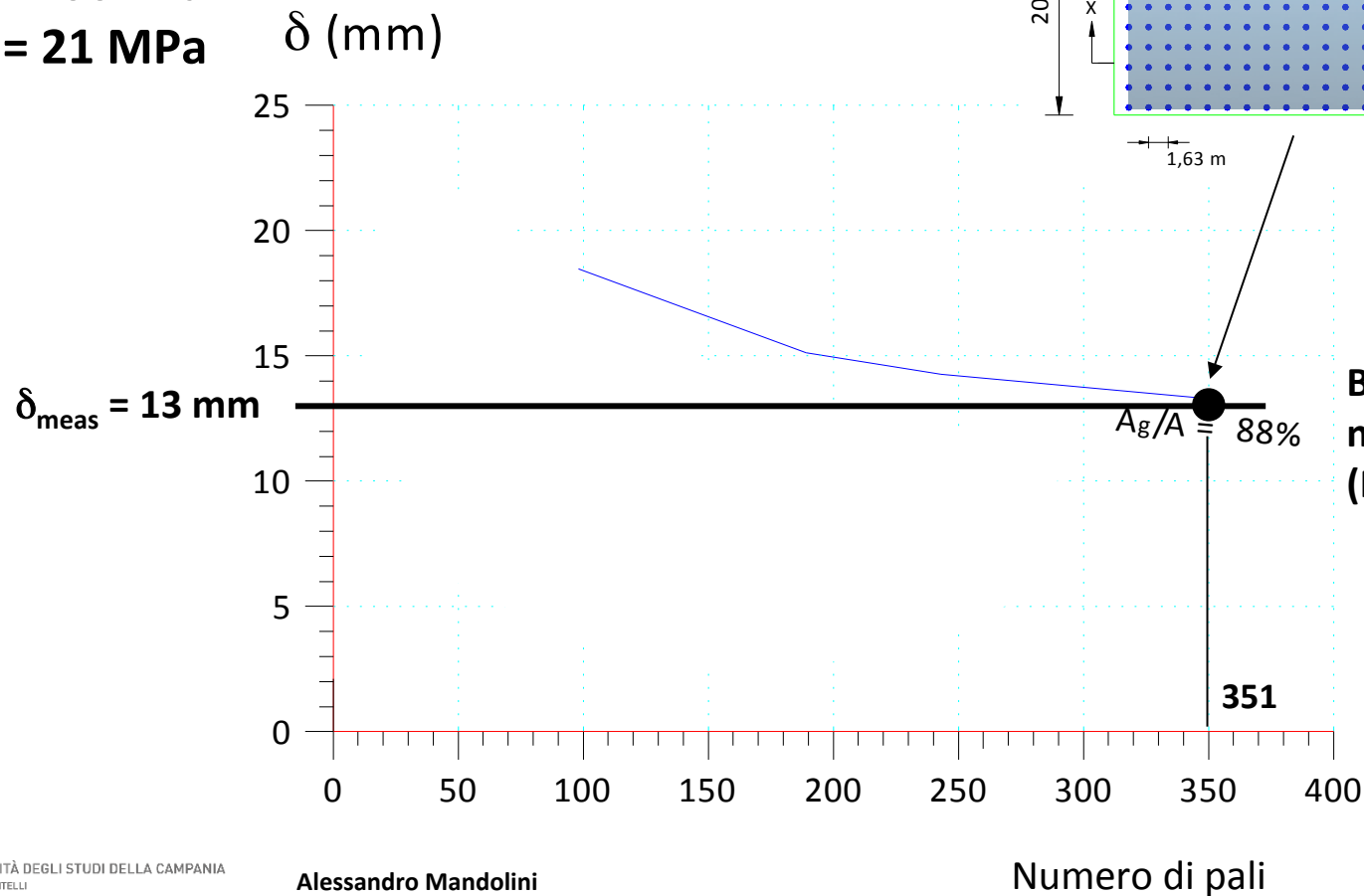


Back-analysis by  
numerical model  
(NAPRA)



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London clay:  
 $c_u \sim 100$  kPa  
 $G_0 = 21$  MPa



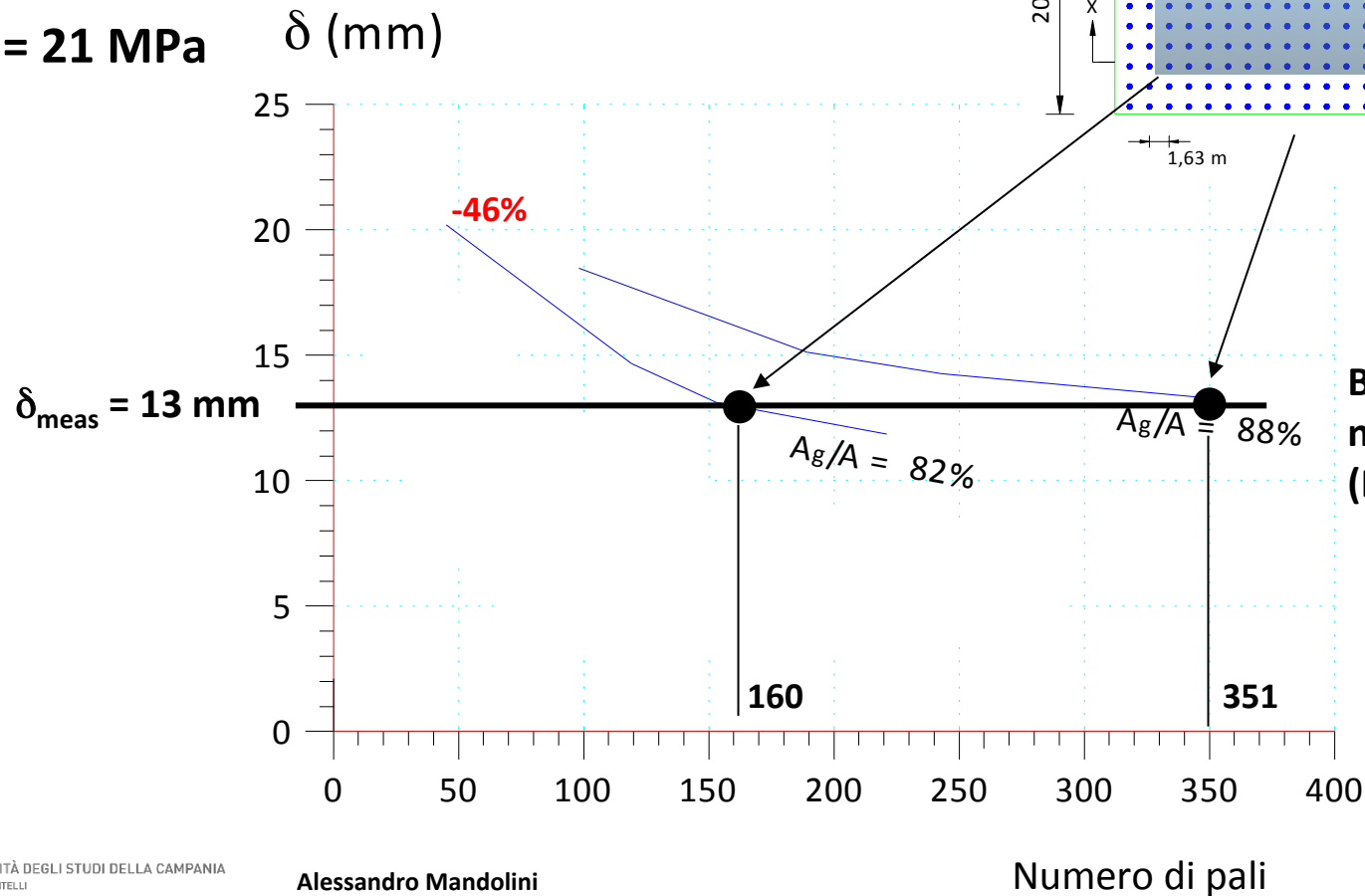
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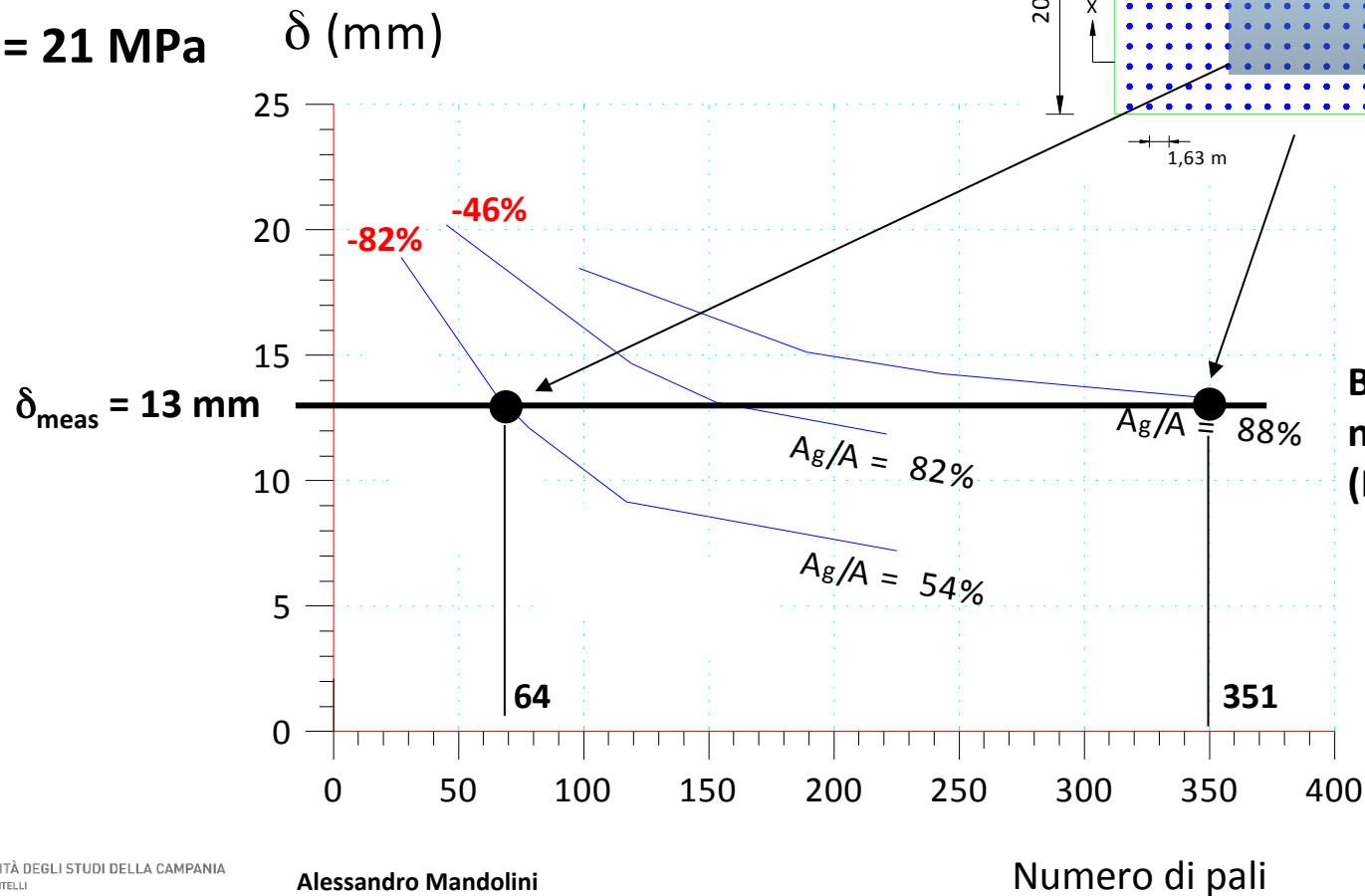


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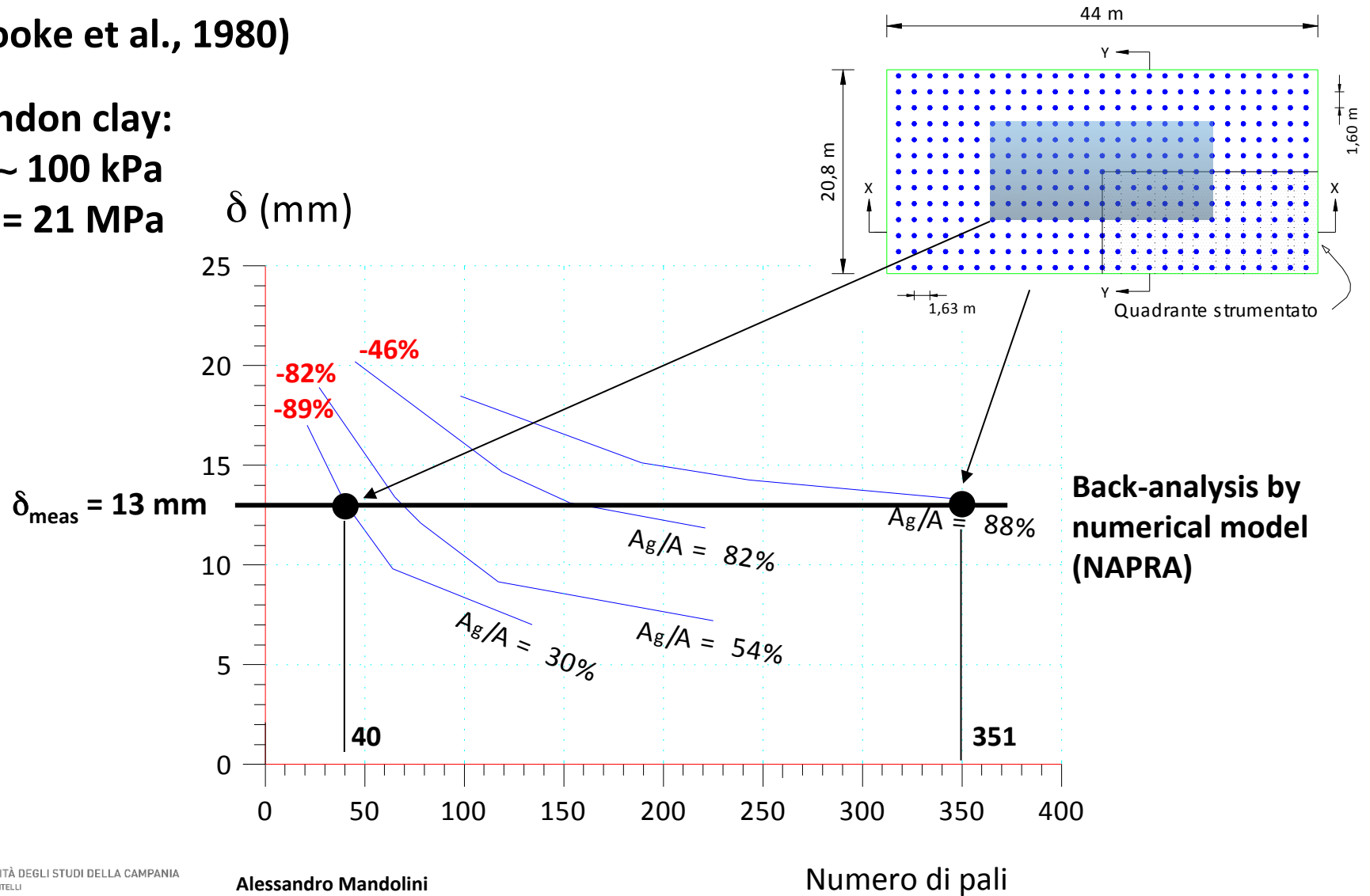


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numerical model  
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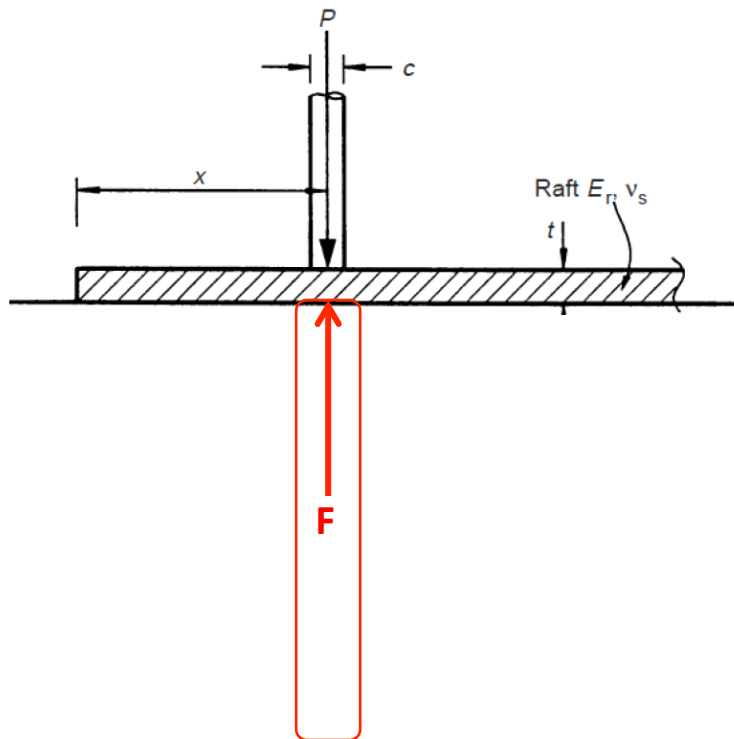
London clay:  
 $c_u \sim 100$  kPa  
 $G_0 = 21$  MPa



Back-analysis by  
numerical model  
(NAPRA)



## Reducing differential settlement: benefit on bending moment and shear forces in the raft



### The concept

For given conditions,  $M$  and  $T$  will increase as  $P$  increases.

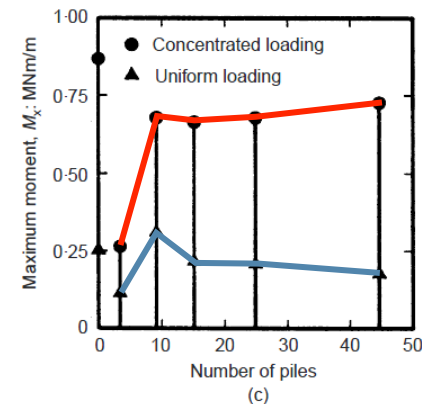
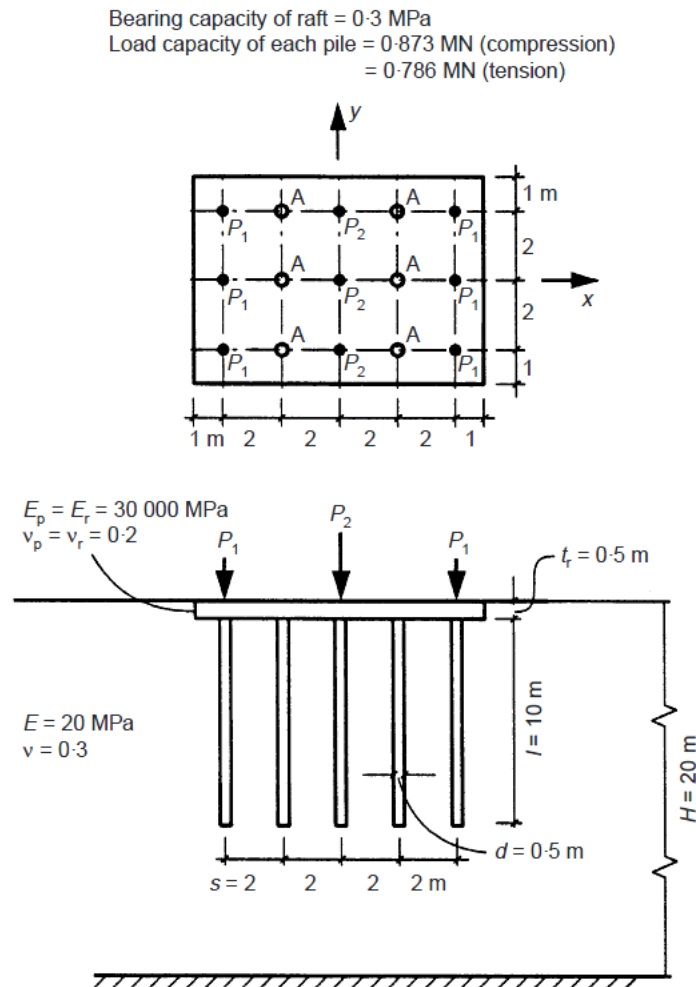
Piles placed just underneath the column and working at a load  $F$  will help to reduce the state of the stress into the raft at some distance  $x$ .



# Reducing differential settlement: benefit on bending moment and shear forces in the raft

Theoretical example by Poulos (2001):

only 3 piles strategically located give the best performance in terms of bending moment  $M$

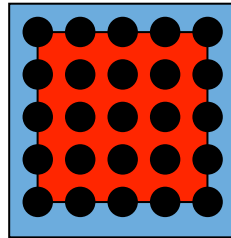
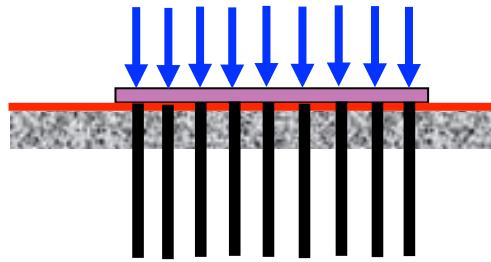


~ 1/3 for concentrated loading

~ 1/2 for uniform loading



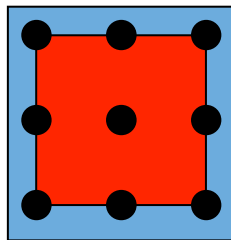
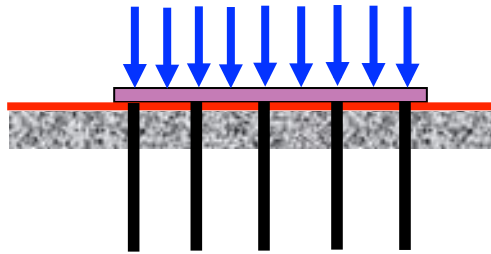
# Different layouts for large piled rafts ( $B/L > 1$ )



$$A_G/A \rightarrow 1$$

$s/d$  small

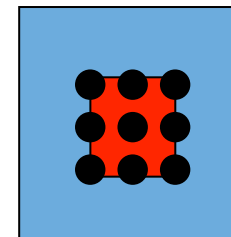
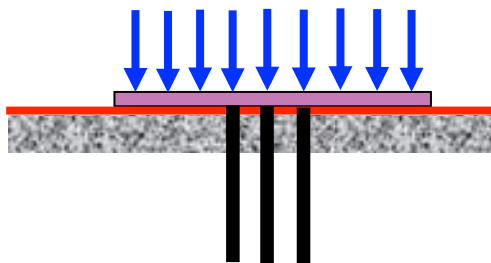
**CONVENTIONAL**



$$A_G/A \rightarrow 1$$

$s/d$  large

**OPTIMIZED, but not necessarily effective**



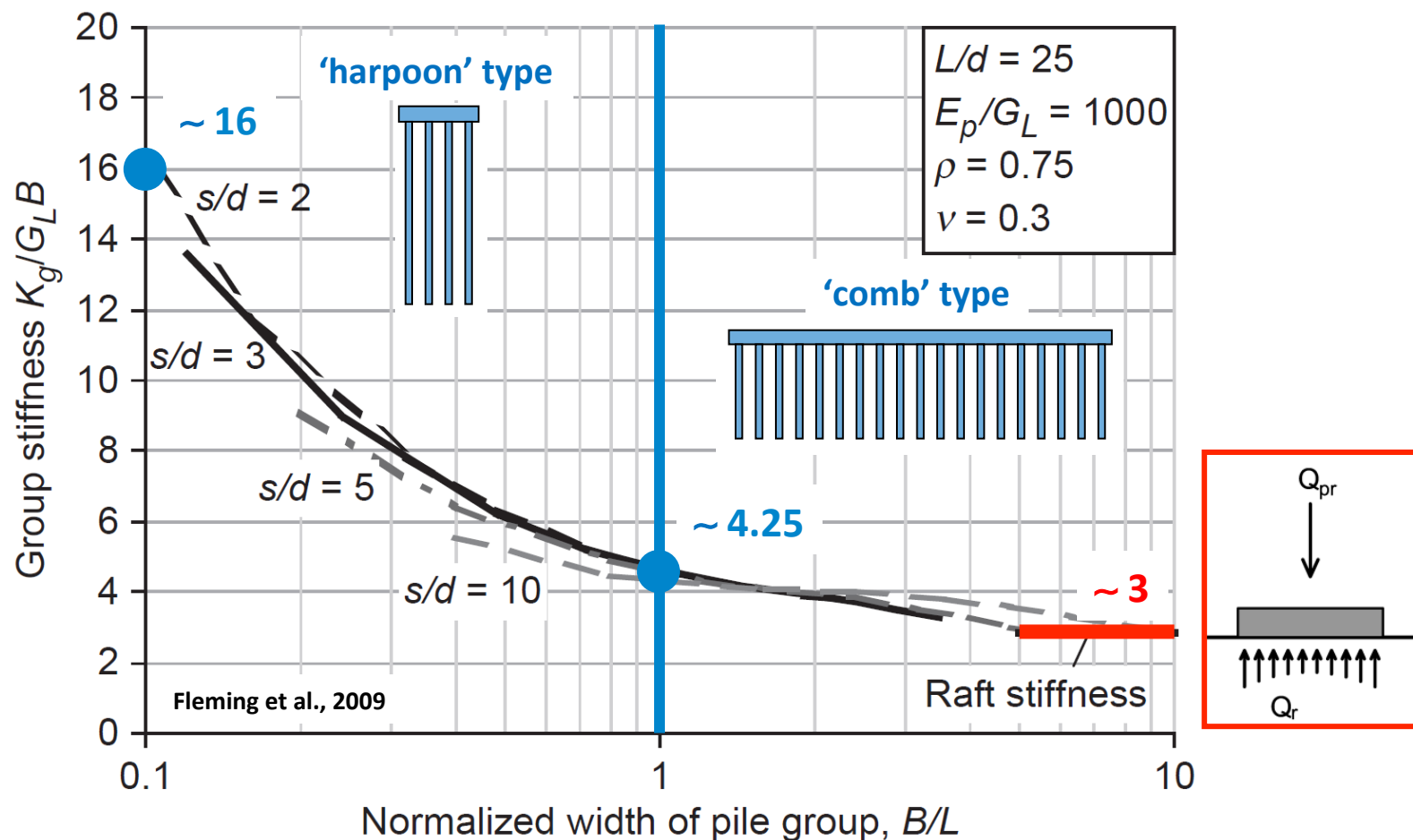
$$A_G/A < 1$$

$s/d$  small

**OPTIMIZED, effective for reducing  $\Delta w$  and  $M$**

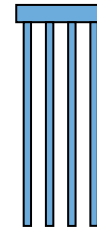


If the ratio  $B/L$  is small enough (say  $B/L < 1$ ), adding piles is more and more effective in increasing stiffness ( $16/3 \sim 5.3$ ).



It is the case of small structures (small B) for which is relatively easy to have  $B/L < 1$ .

'harpoon' type



### EXAMPLE

$B = 10 \text{ m}$

$L = 20 \text{ m}$

$d = 0.5 \text{ m}$

$s = 2 \text{ m (4d)}$

$N = 25 \text{ piles}$

$$K \downarrow G / G \cdot B = 5.2$$

**25 medium dia. piles**

**(total length 500 m)**

**to reduce average settlement by 70%**





It is the case of small structures (small B) for which is relatively easy to have  $B/L < 1$ .

### EXAMPLE

B = 10 m

L = 30 m

d = 0.5 m

s = 4 m (8d)

N = 9 piles

$$K \downarrow G / G \cdot B = 7.5$$

'harpoon' type

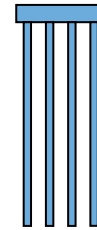


**9 medium dia. piles, but more spaced and longer,  
(total length ~ 1/2 of the previous solution)  
have the same effects!!!!**



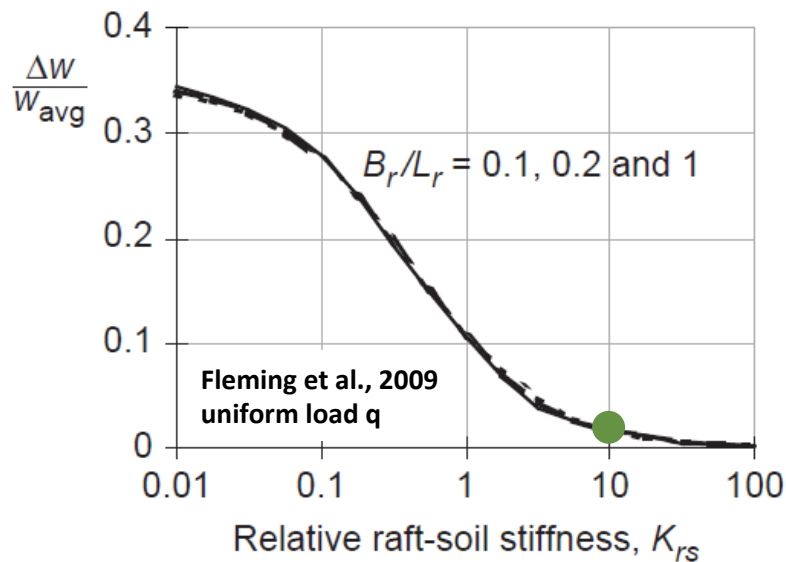
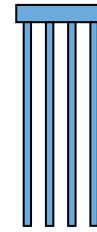
**In the case of small structures  
(small B), piles can greatly help to  
reduce average settlement.**

**'harpoon' type**



**Differential settlement is not a major problem. If the case, it can be tackled by adopting reasonable raft thickness.**

'harpoon' type



### EXAMPLE

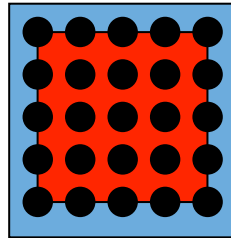
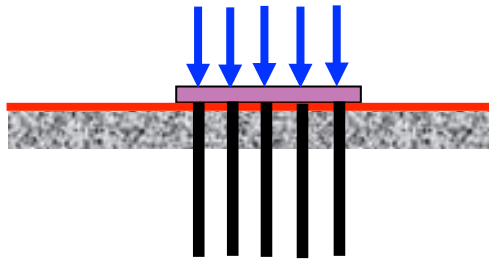
$B_r = 10 \text{ m}; L_r = 10 \text{ m}; E_r/E_s = 250$   
 $\nu_s = 0.30; \nu_r = 0.15$

$\Delta w/w_{avg} \sim 0 \text{ (} K_{rs} = 10 \text{)} \rightarrow$   
 $t_r \sim 2 \text{ m}$

$$K_{rs} = 5.57 \frac{E_r}{E_s} \frac{1 - \nu_s^2}{1 - \nu_r^2} \left( \frac{B_r}{L_r} \right)^{0.5} \left( \frac{t_r}{L_r} \right)^3$$



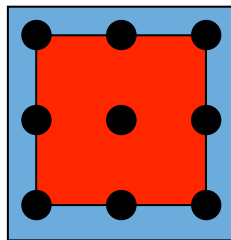
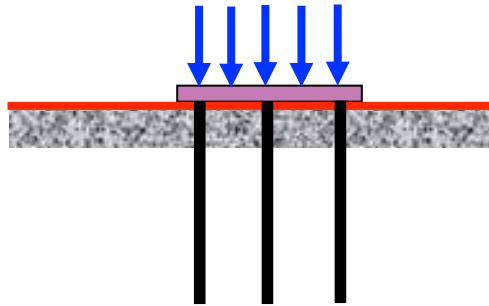
## Different layouts for small piled rafts ( $B/L < 1$ )



$$A_G/A \rightarrow 1$$

$s/d$  small

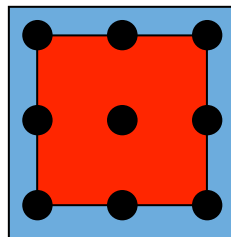
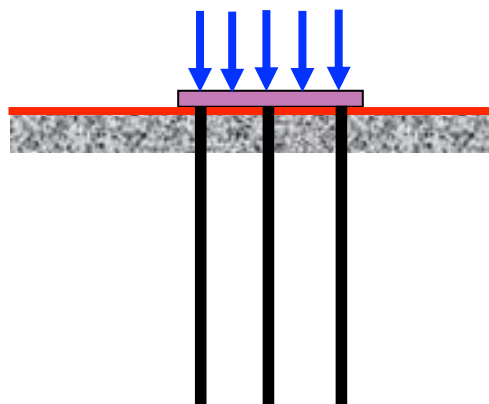
**CONVENTIONAL**



$$A_G/A \rightarrow 1$$

$s/d$  large  
 $B/L \sim 0.5 \div 0.7$

**OPTIMIZED, effective  
for reducing  $w$**



$$A_G/A \rightarrow 1$$

$s/d$  large  
 $B/L \sim 0.3 \div 0.4$

**OPTIMIZED, larger  
impact in reducing  $w$**



**The decision of using piles can be also due to poor bearing capacity of the raft.**



**The decision of using piles can be also due to poor bearing capacity of the raft.**

$$q_{lim} = F_q \cdot N_q \cdot \sigma_{vD} + F_c \cdot N_c \cdot c + F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$



The decision of using piles can be also due to poor bearing capacity of the raft.

$$q_{lim} = \cancel{F_q \cdot N_q \cdot \sigma_{vD}} + F_c \cdot N_c \cdot c + F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$

For sake of simplicity, in the following the term related to foundation depth will be neglected.



$$q_{lim} = F_c \cdot N_c \cdot c + F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$

**In fine grained soils (clay, silty clay), undrained conditions are generally those governing bearing capacity problem:**

$$q_{lim} \approx 6 \cdot c_u$$

**In coarse grained soils (sand, gravel), only drained conditions have to be considered:**

$$q_{lim} \approx F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$





$$q_{lim} \approx 6 \cdot c_u$$

$$q_{lim} \approx F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$

According to local Codes, maximum applied load is defined as:

$$q_{max} \approx \frac{6 \cdot c_u}{FS}$$

$$q_{lim} \approx \frac{F_\gamma \cdot N_\gamma \cdot \gamma \cdot B}{2 \cdot FS}$$

Assuming  $FS = 3$ , it is simple to demonstrate that:

**in fine grained soils, it is possible to build structures corresponding to uniform loads ranging from few tens of kPa (n.c.) to few hundreds of kPa (o.c.).**



$$q_{lim} \approx 6 \cdot c_u$$

$$q_{lim} \approx F_\gamma \cdot N_\gamma \cdot \gamma \cdot \frac{B}{2}$$

According to local Codes, maximum applied load is defined as:

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$$q_{lim} \approx \frac{F_\gamma \cdot N_\gamma \cdot \gamma \cdot B}{2 \cdot FS}$$

Assuming  $FS = 3$ , it is simple to demonstrate that:

in coarse grained soils, it is possible to build structures corresponding to uniform loads ranging from few hundred of kPa (loose and n.c.) to few thousands of kPa (dense and o.c.).



# The minimum factor of safety (FS = 3) is often, to not say very often, guaranteed

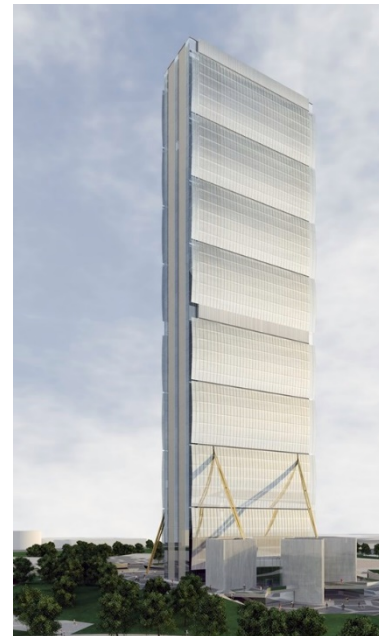
**n.c. clay**  
few tens of meters



**o.c clay**  
tens of meters



**Loose n.c sand**  
few hundreds of meters



**Dense o.c. sand**  
hundreds of meters



# Other benefit from adopting spaced piles ?



## Two fundamental parameters:

- Pile group efficiency at failure
- Piled raft efficiency at failure

$$\eta_{\downarrow PG} = R_{\downarrow PG} / R_{\downarrow S}$$

$$\beta_{\downarrow PR} = R_{\downarrow PR} / R_{\downarrow PG}$$

$R_{PR}$  = piled raft resistance

$R_{PG}$  = pile group resistance

$R_S$  = single pile resistance



**Cooke (1986): *Piled raft foundations on stiff clays—a contribution to design philosophy***  
**Géotechnique, vol. 36(2)**

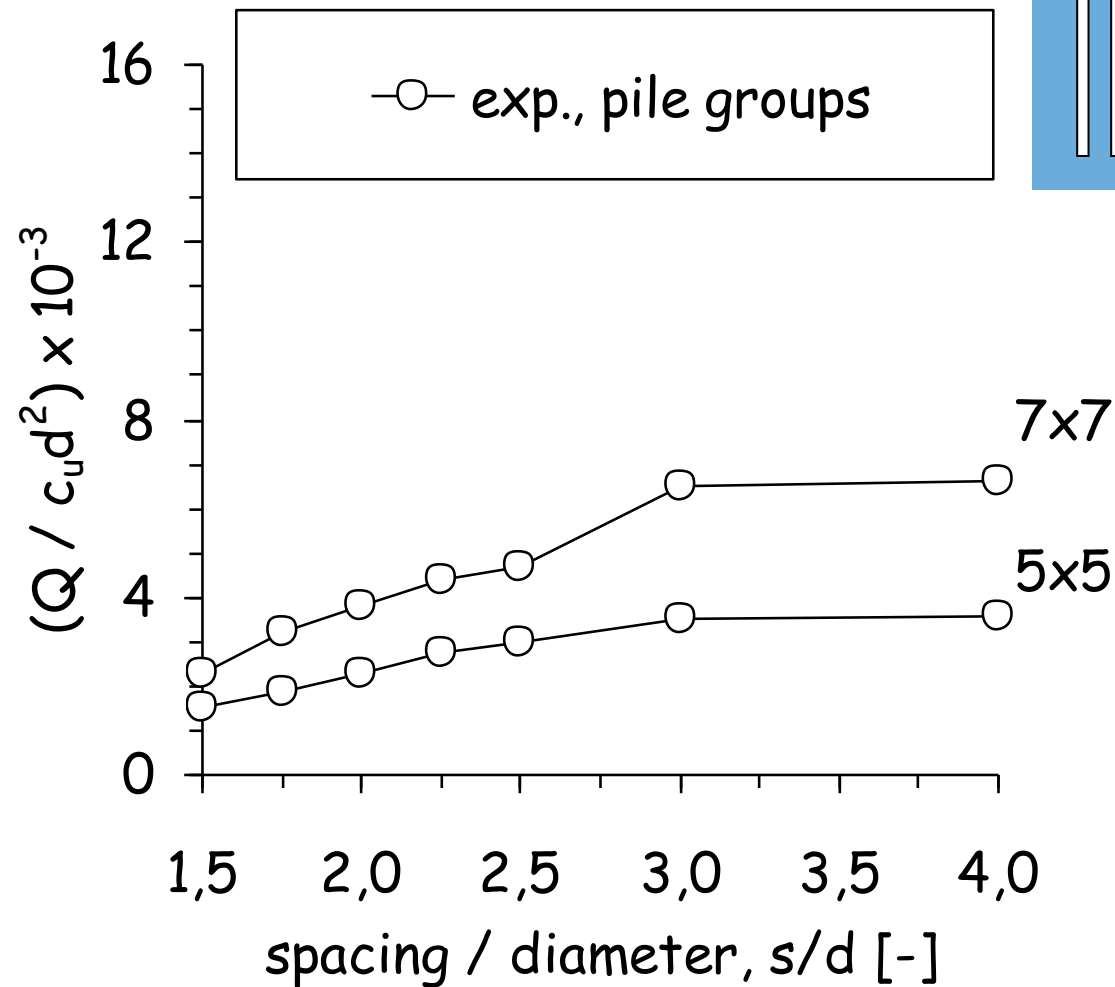
rem. London clay - 1-g lab model

$N = 3^2, 5^2, 7^2, 9^2$

$L/d = 24, 48$

$s/d \leq 4$

$w = 10\%B$



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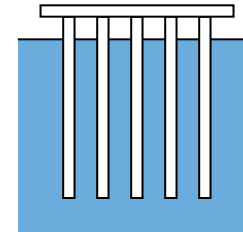
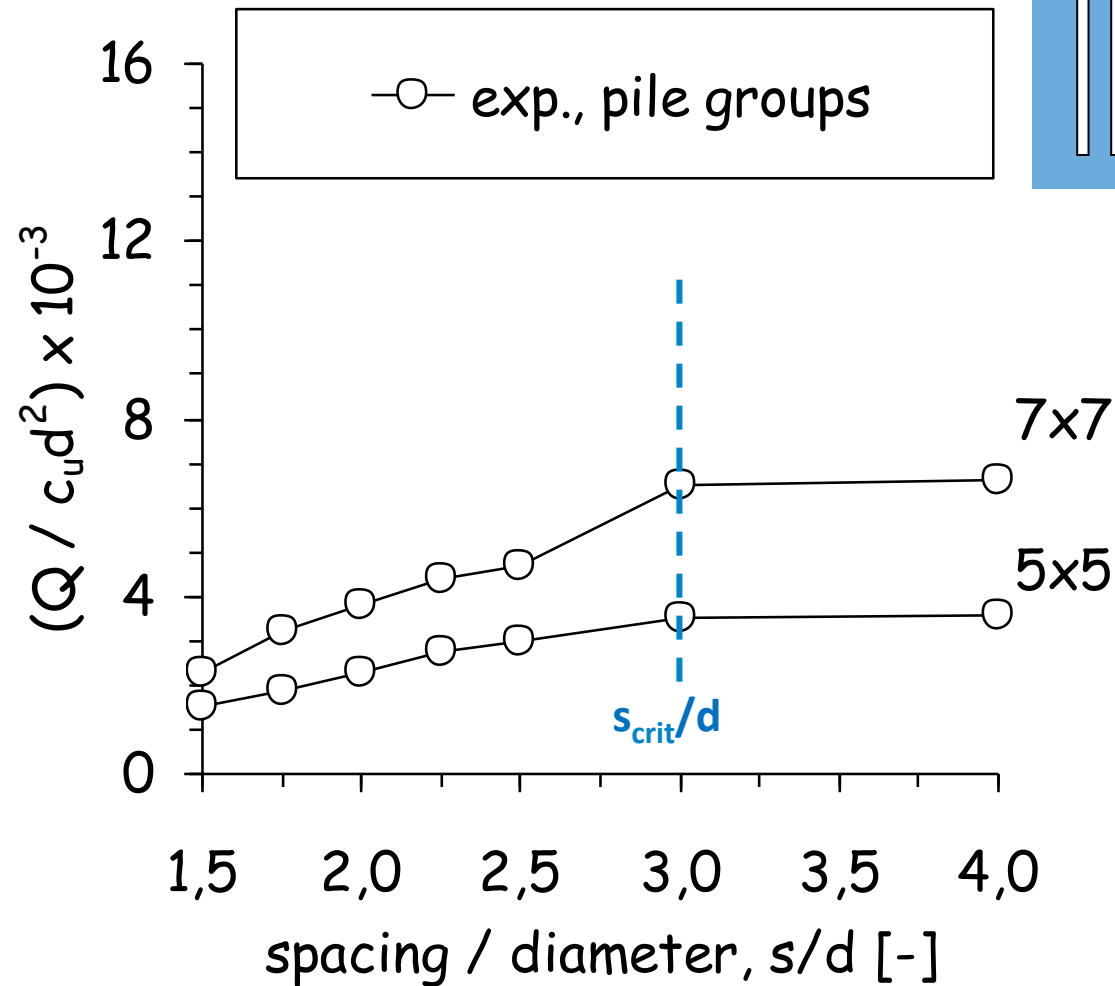
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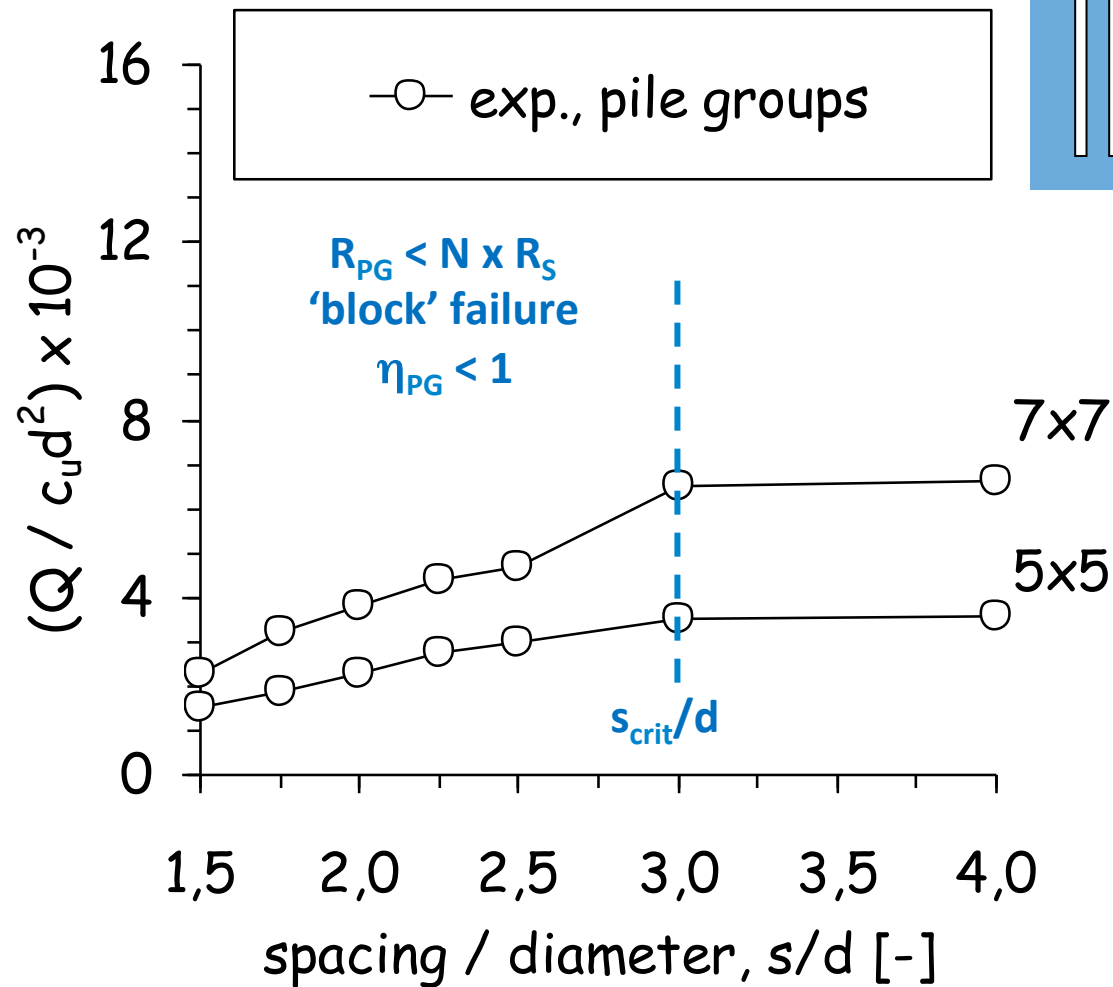
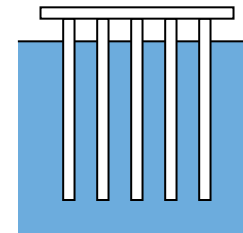
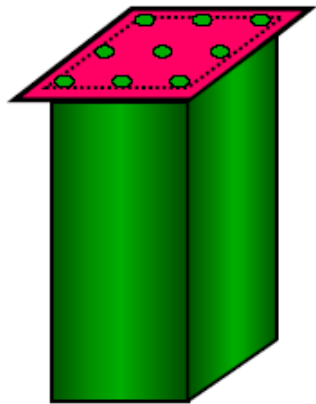
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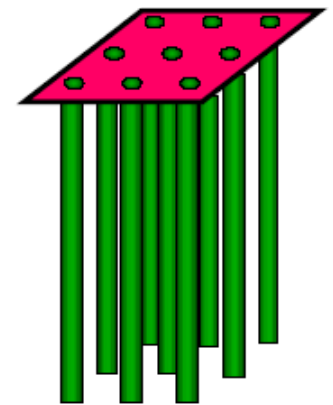
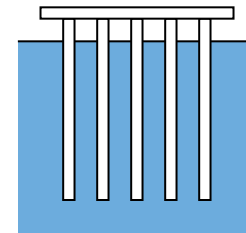
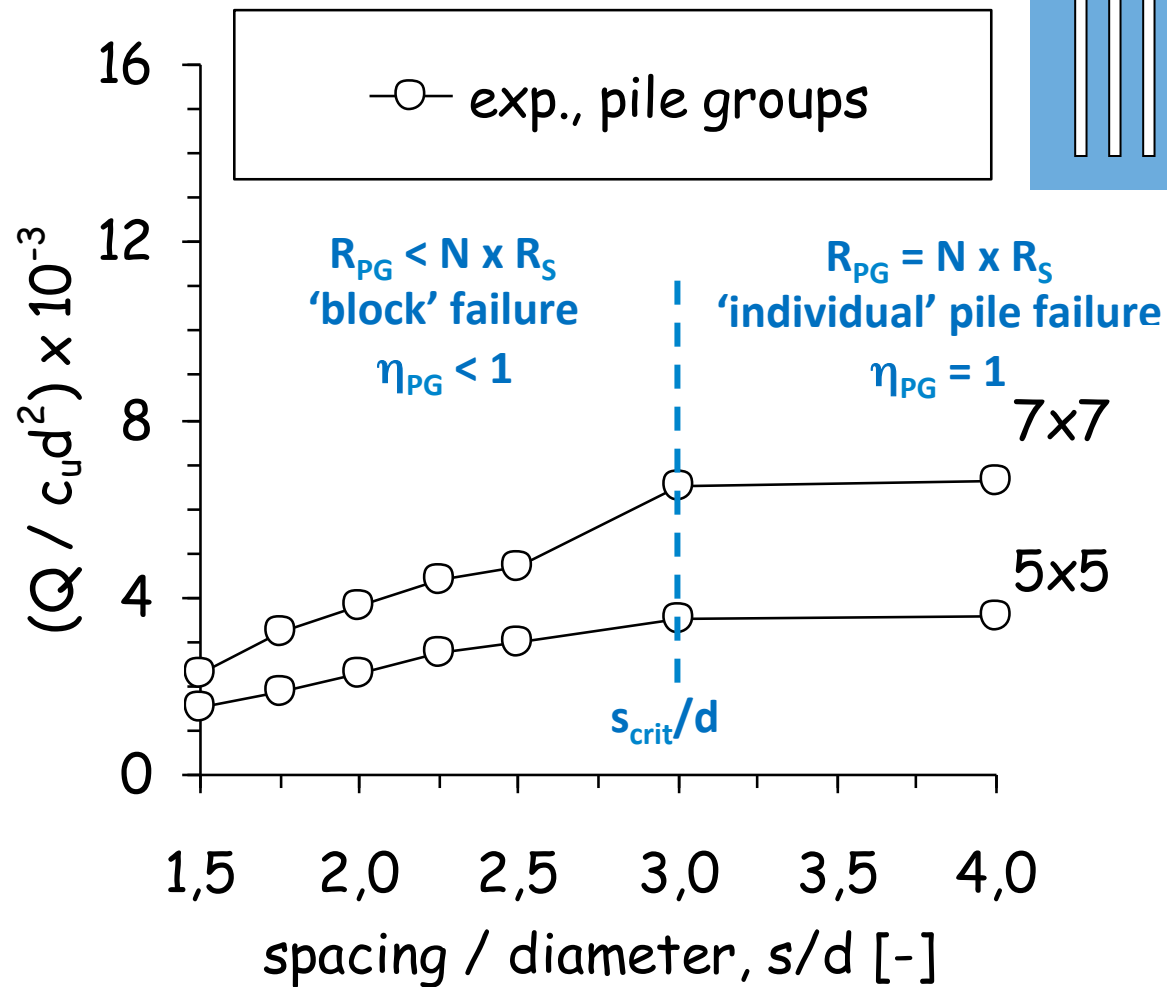
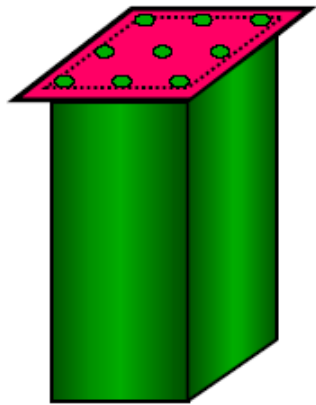
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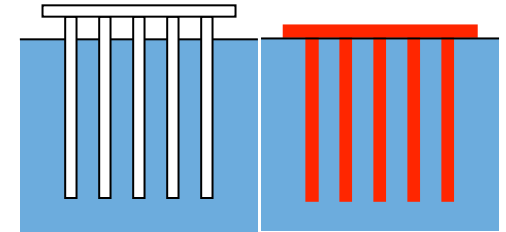
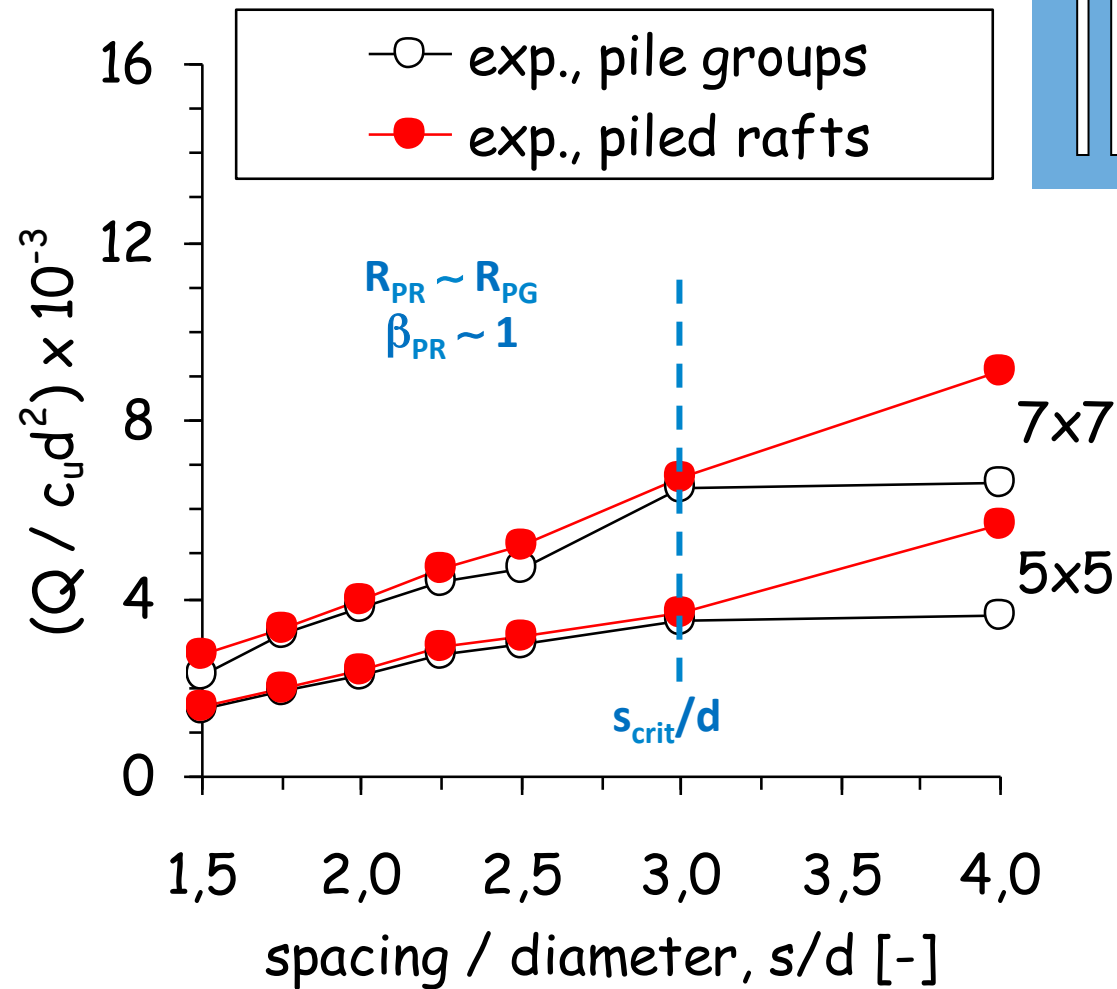
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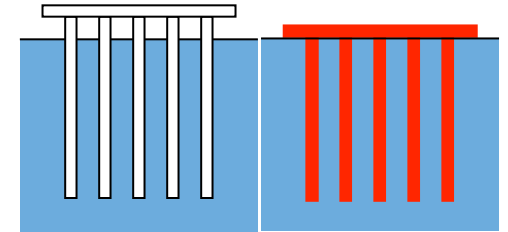
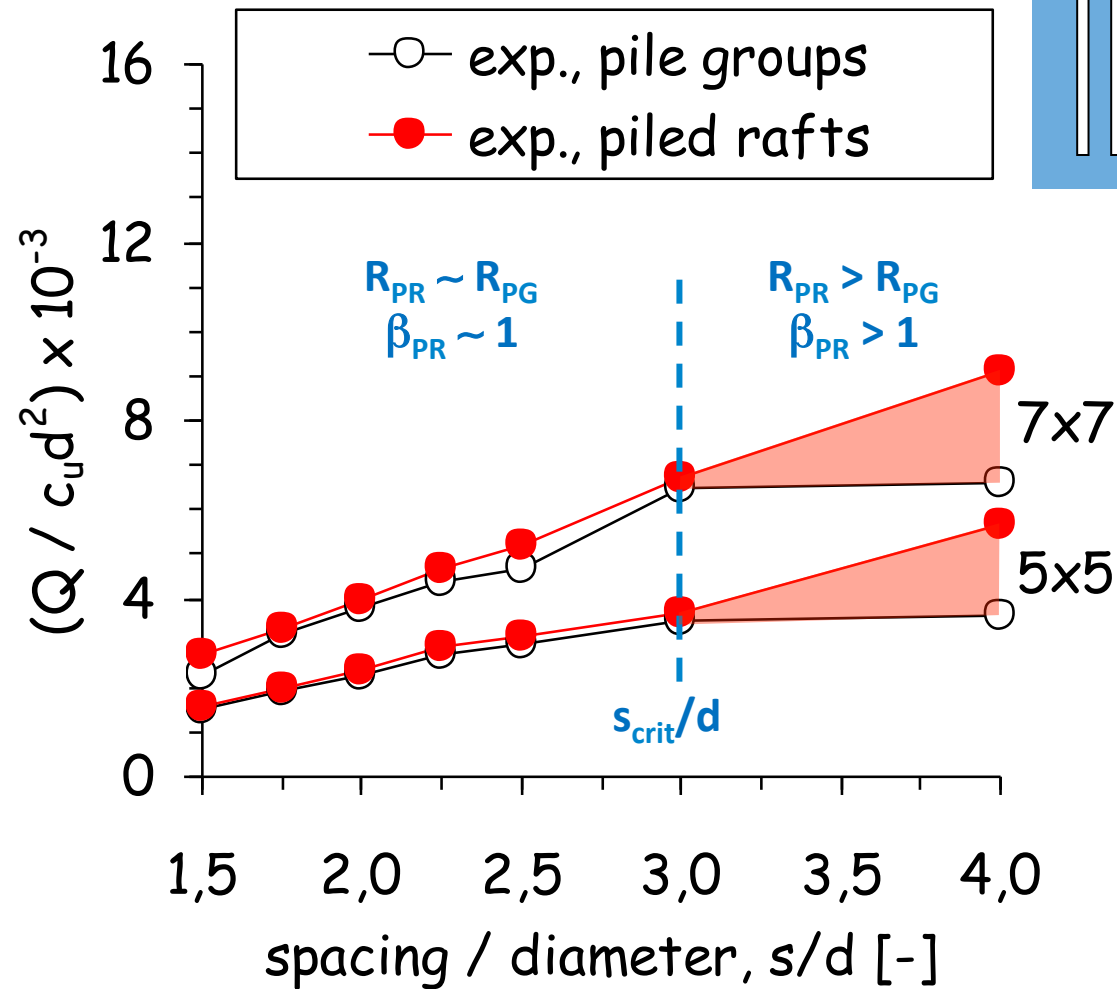
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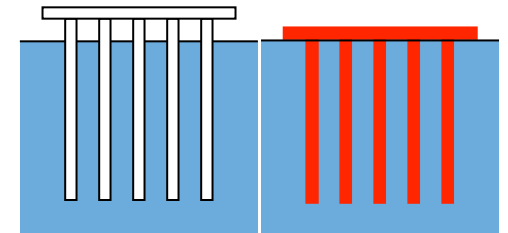
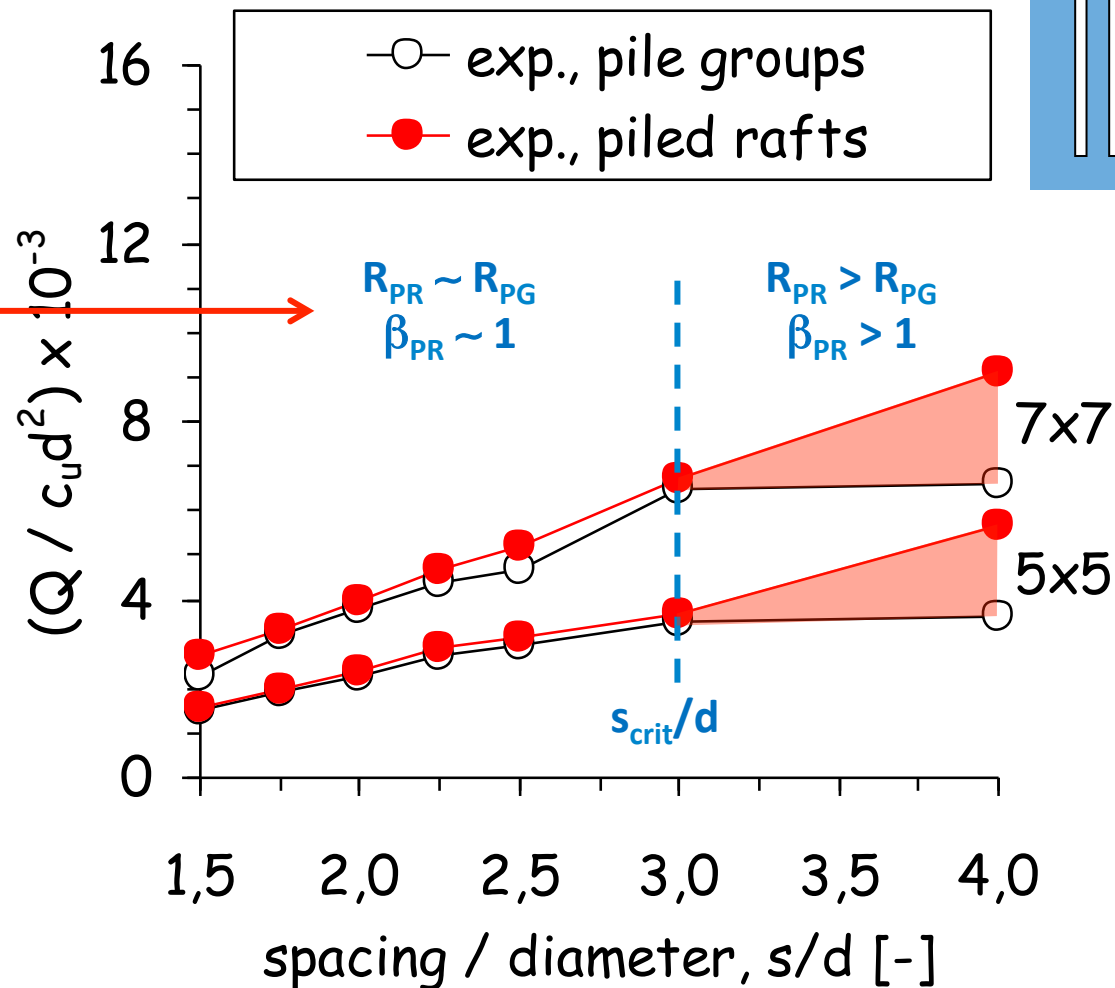
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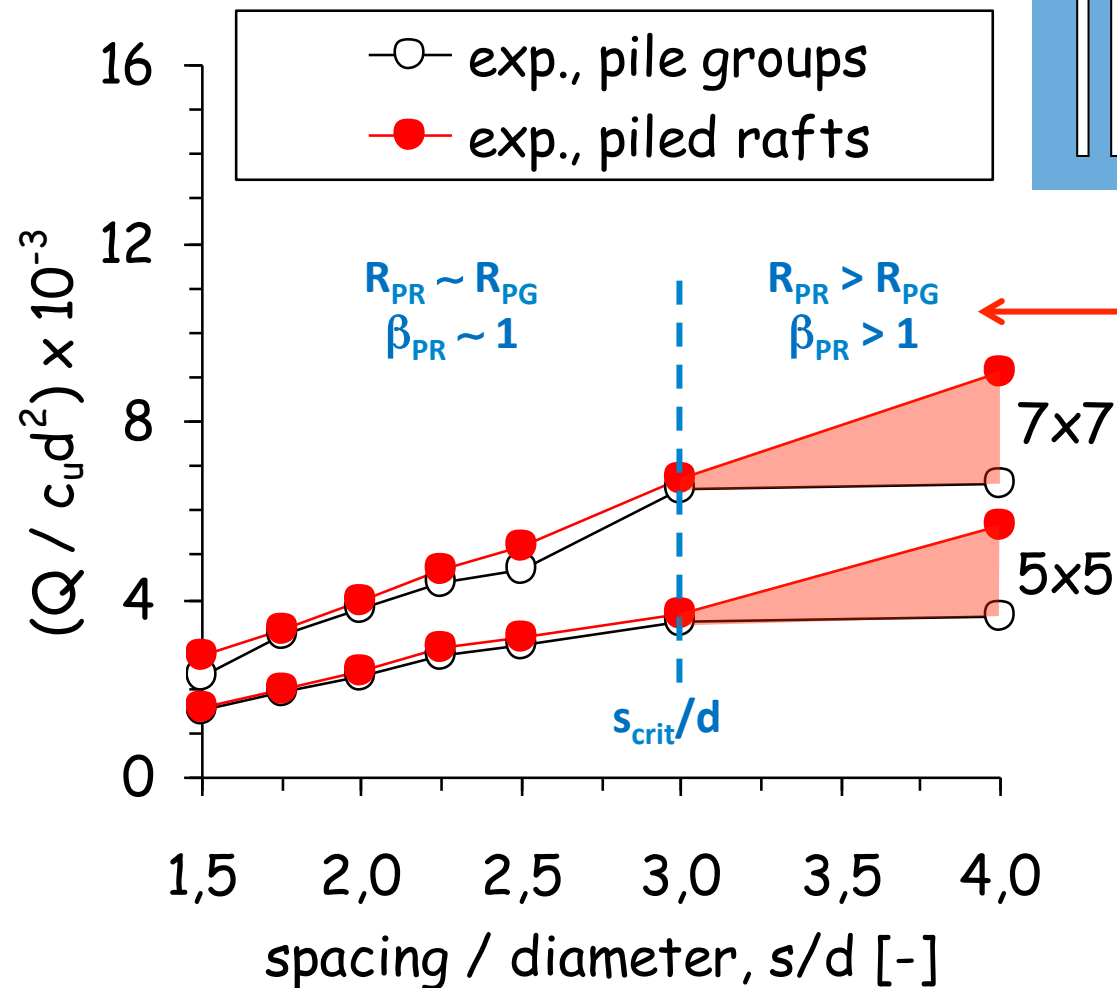
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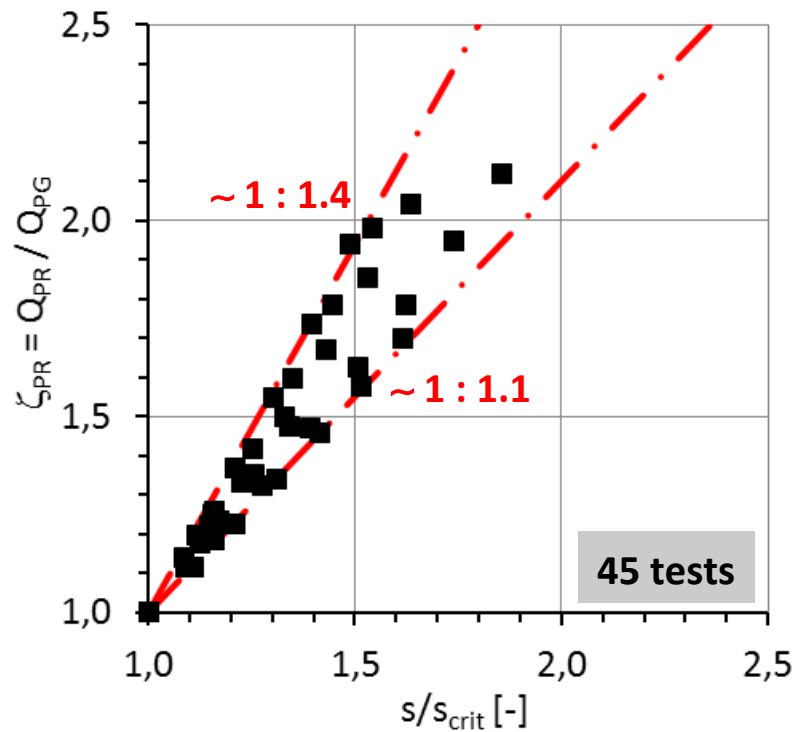
**SHIELD EFFECT:** For spacing smaller than some critical value (that inducing 'block' failure), the raft is inhibited in contributing to the overall resistance of the piled raft



**RAFT ENHANCING PILE GROUP:** For spacing larger than some critical value (that inducing 'block' failure), the raft cooperates with piles in increasing the overall resistance of the piled raft



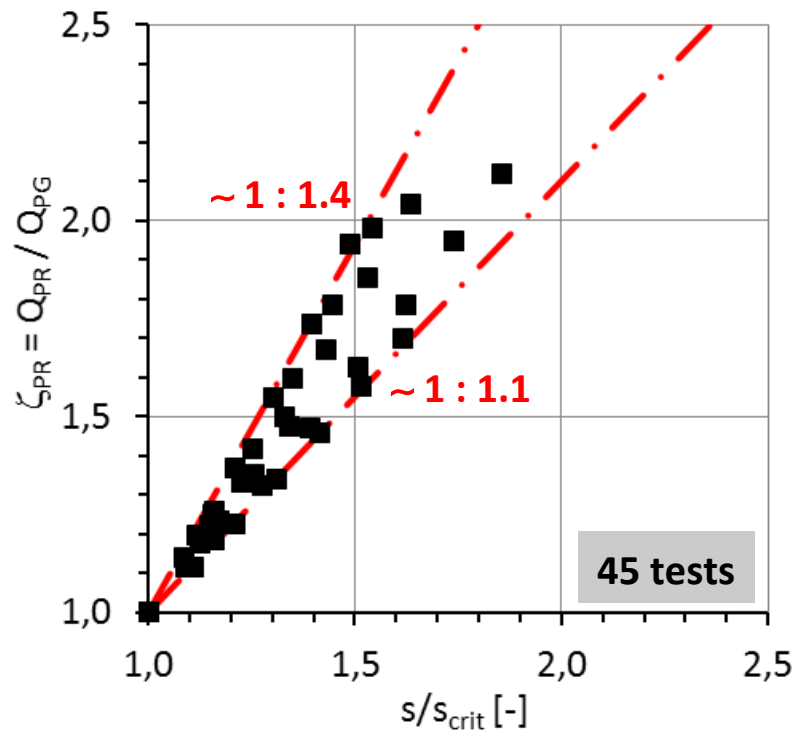
**Cooke (1986): *Piled raft foundations on stiff clays—a contribution to design philosophy***  
**Géotechnique, vol. 36(2)**



**Piled raft resistance ( $R_{PR}$ ) from 10% to 40% greater than that of Pile Group alone ( $R_{PG}$ ), with pile spaced at  $s \geq s_{crit}$ , due to raft-soil contact.**



Cooke (1986): *Piled raft foundations on stiff clays—a contribution to design philosophy*  
Géotechnique, vol. 36(2)



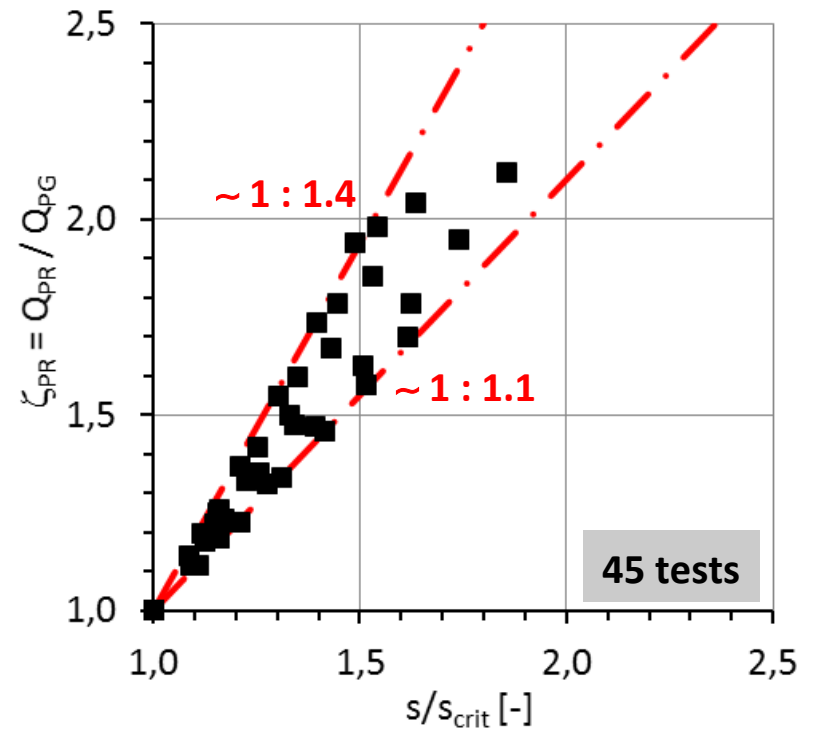
Piled raft resistance ( $R_{PR}$ ) from 10% to 40% greater than that of Pile Group alone ( $R_{PG}$ ), with pile spaced at  $s \geq s_{crit}$ , due to raft-soil contact.

**Consequence on design:  
LESS PILES**



# SUMMARY

Piles should be installed at **spacing  $s$  larger than critical value  $s_{crit}$**  (preventing 'block' failure mode) in order to allow the raft to positively contribute to overall resistance of a piled raft ( $\zeta_{PR} > 1$ ).

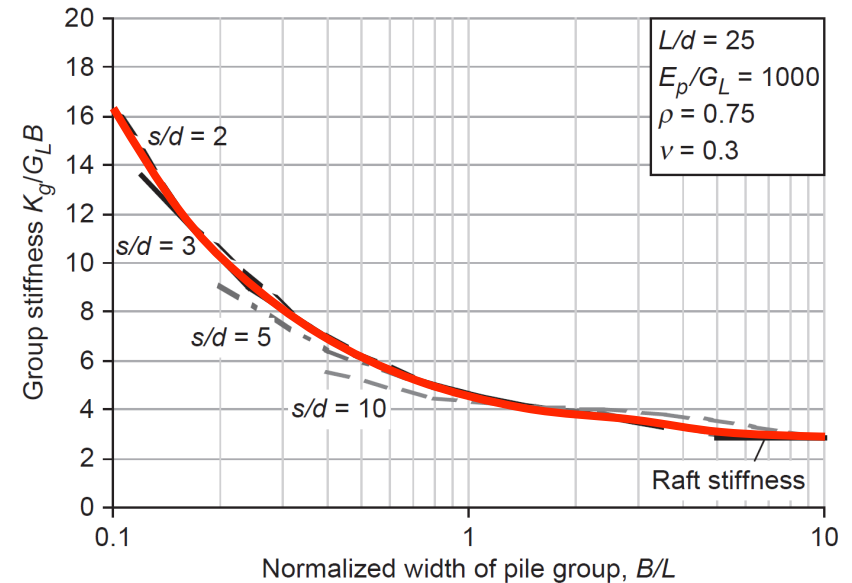




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**More spaced** piles do not compromise the overall stiffness being the pile group stiffness almost constant for given  $s/d$ .

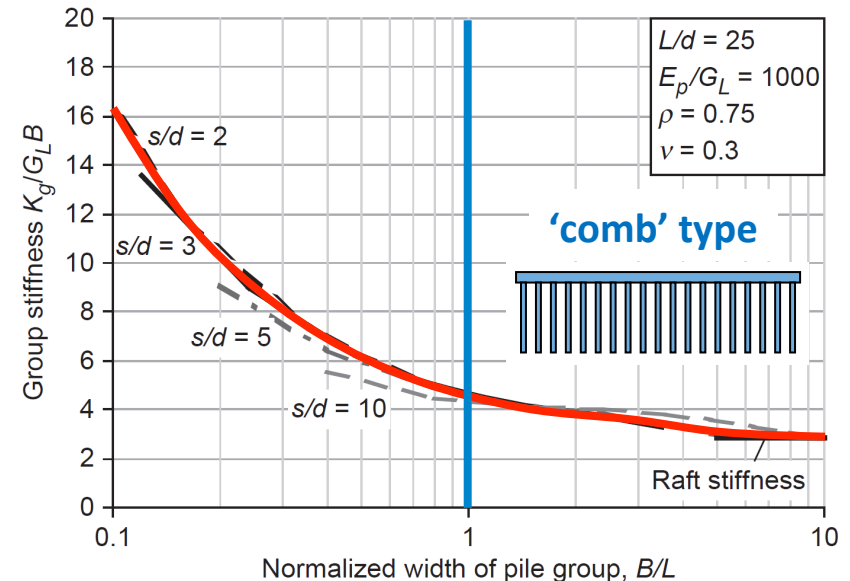


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For large raft ('comb' type,  $B/L > 1$ ), typically the unpiled raft has enough resistance. Adding **piles** is **not** very **effective** to **reduce average settlement**.



# SUMMARY

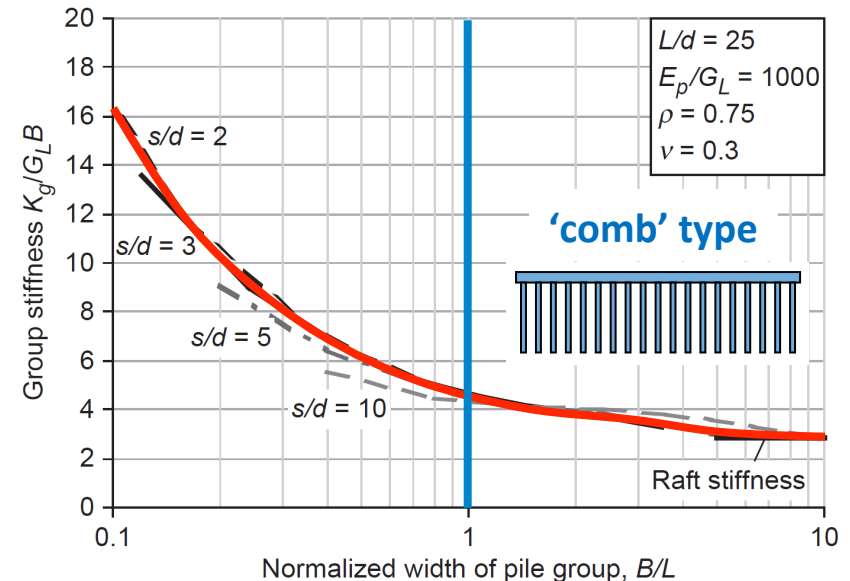
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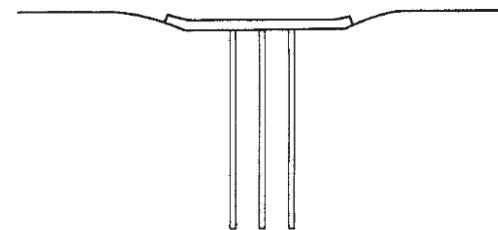
For **large raft ('comb' type,  $B/L > 1$ )**, typically the unpiled raft has enough resistance. Adding **piles is not very effective to reduce average settlement**.

If strategically placed below the raft, **piles can greatly help to reduce differential settlement (DSBD)**, not practically achievable by increasing raft thickness.

**Also bending moments and shear forces in the raft are reduced (RBD).**



(a) Dishing of unpiled raft



(b) Effect of settlement reducing piles



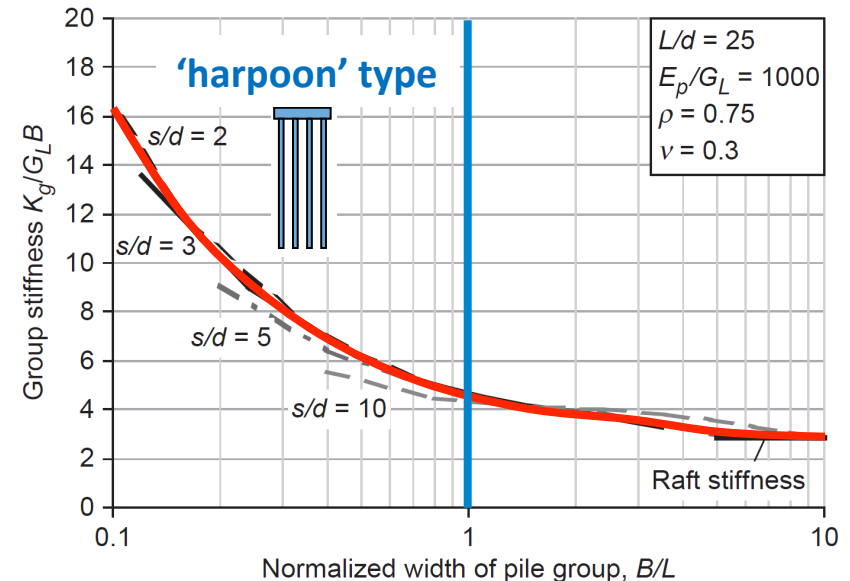
# SUMMARY

Piles should be installed at **spacing  $s$  larger than critical value  $s_{crit}$**  (preventing 'block' failure mode) in order to allow the raft to positively contribute to overall resistance of a piled raft ( $\zeta_{PR} > 1$ ).

**More spaced** piles do not compromise the overall stiffness being the pile group stiffness almost constant for given  $s/d$ .

For **small raft** ('harpoon' type,  $B/L < 1$ ), the use of piles can derive from ULS problem. In these cases, **piles adequately spaced can take advantage from the raft-soil contact to increase the overall resistance and to reduce average settlement (CSBD).**

The reduction of differential settlement can be easily obtained by increasing raft thickness within practical range.



# **‘CHEF RECIPE’ FOR AN OPTIMAL DESIGN APPROACH**



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DESIGN EDILIZIA E AMBIENTE

**Alessandro Mandolini**  
**Design options for piled rafts:**  
**an overview**

# **‘CHEF RECIPE’ FOR AN OPTIMAL DESIGN APPROACH**

**PILES SHOULD BE AS LONG AND  
SPACED AS POSSIBLE AND  
STRATEGICALLY LOCATED WHERE  
LARGER SETTLEMENTS OF THE  
UNPILED RAFT ARE EXPECTED**



## Simple approach to static and seismic design of piled rafts

Mandolini, A.<sup>(1)</sup>, Di Laora, R.<sup>(2)</sup> and Iodice, C.<sup>(3)</sup>

<sup>(1)</sup> Università degli Studi della Campania “Luigi Vanvitelli”, Italy

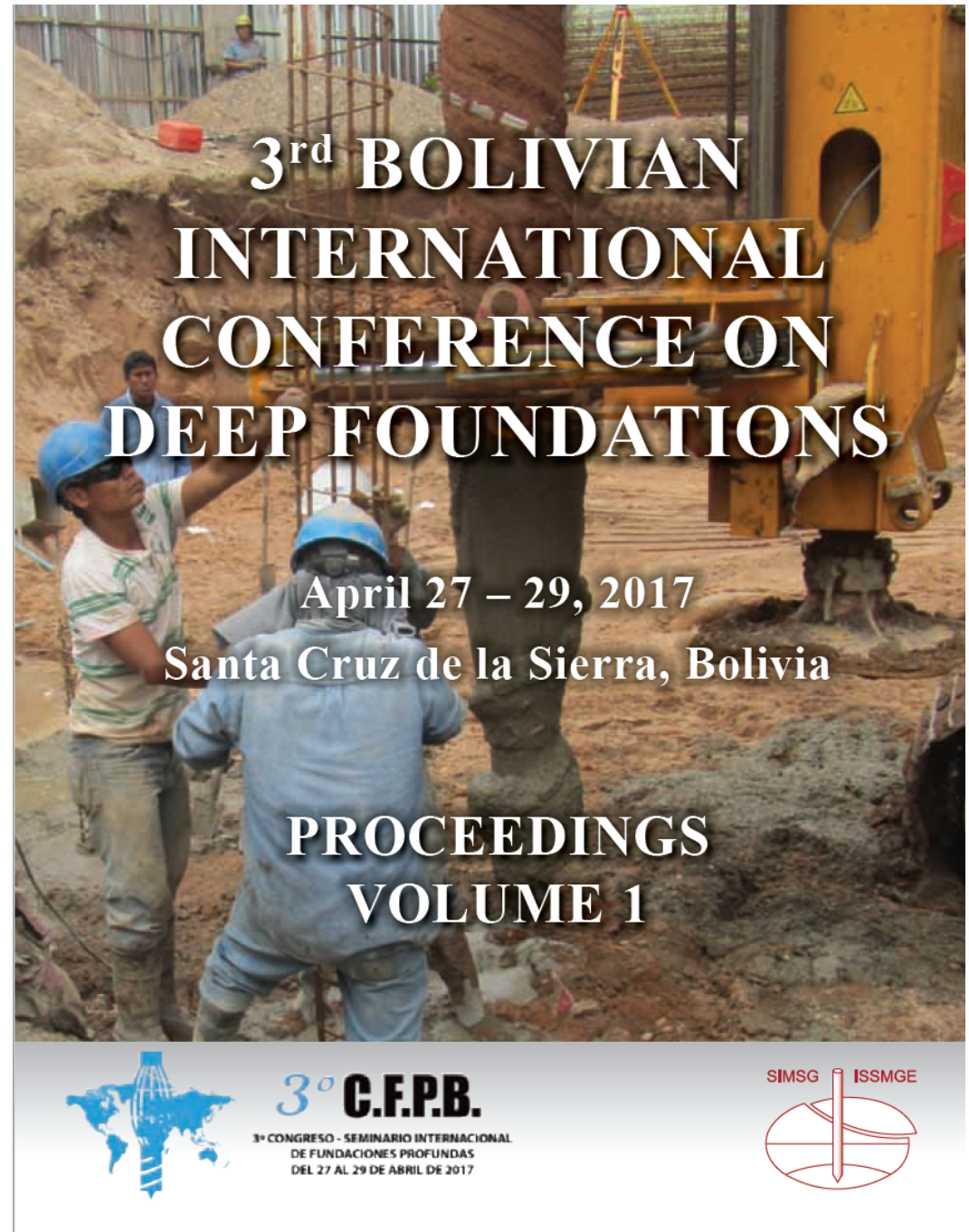
[alessandro.mandolini@unina2.it](mailto:alessandro.mandolini@unina2.it)

<sup>(2)</sup> Università degli Studi della Campania “Luigi Vanvitelli”, Italy [raffaele.dilaora@unina2.it](mailto:raffaele.dilaora@unina2.it)

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**ABSTRACT.** Current design of piled rafts often neglects a number of aspects well known in scientific literature, sometimes leading to increased costs without appreciable increase in performance. This work makes an attempt to partially fill this lack between State of Art and State of Practice; to this end, the paper briefly recalls available simple design methods regarding both geotechnical and seismic issues and proposes a novel simple procedure to estimate the load-settlement curve of a piled raft as well as the load sharing between piles and raft for vertical centered loads. The method has been validated through comparison with numerical and experimental data and applied to a case history; it will be shown that the proposed procedure, despite its simplicity, is able to account for the non-linearity in the soil behavior, the latter being responsible of progressive variation of the load sharing with increasing applied top load. Further, regarding seismic issues, simplified formulae from past works are recalled and discussed.

**... a novel simple procedure to estimate the load-settlement curve of a piled raft as well as the load sharing between piles and raft for vertical centered loads.**

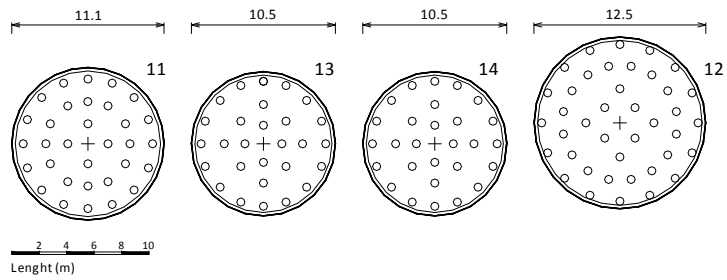


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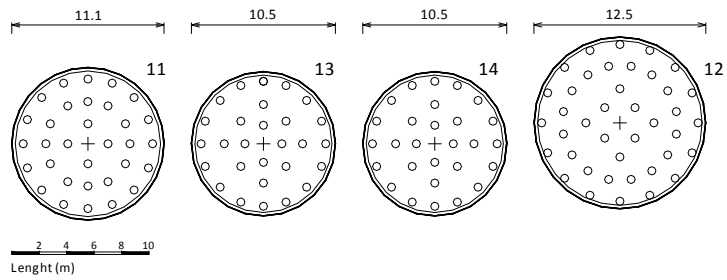


# Original CBD design: 128 piles

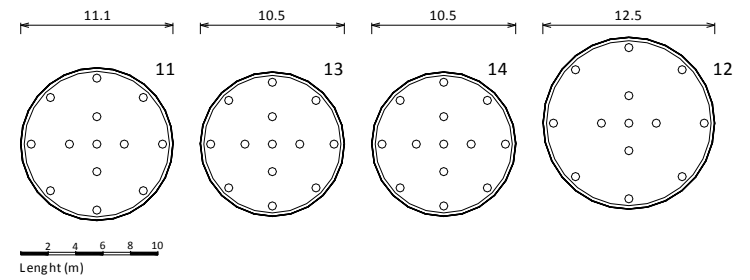




## Original CBD design: 128 piles



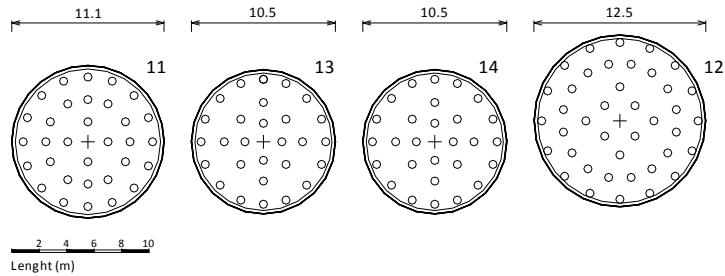
## New SBD design: 52 piles



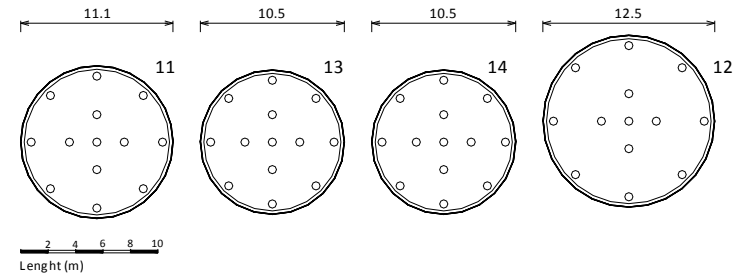
~ 60% less piles



## Original CBD design: 128 piles

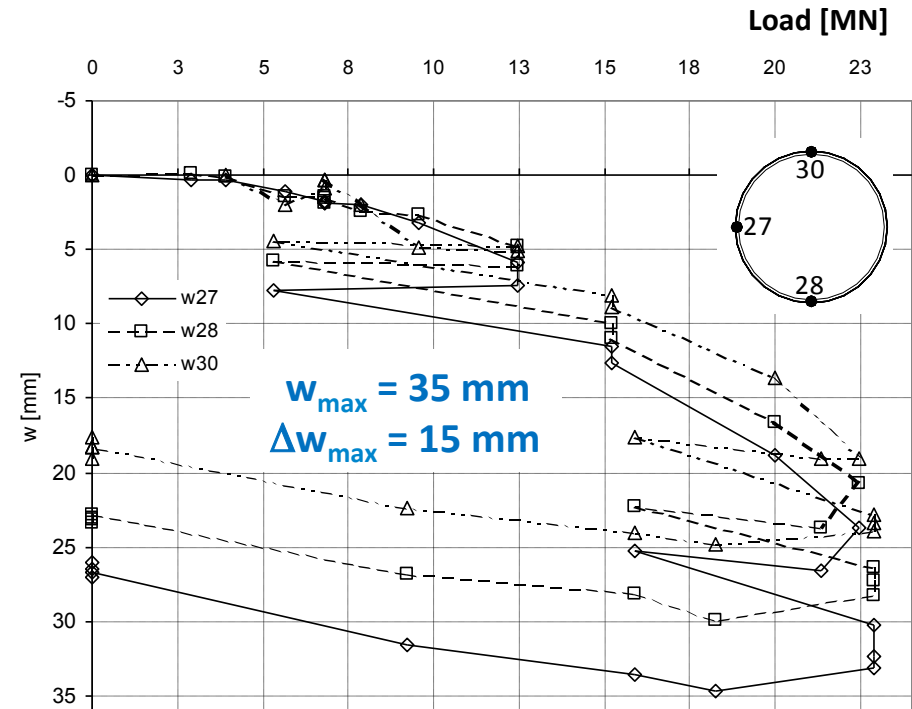


## New SBD design: 52 piles

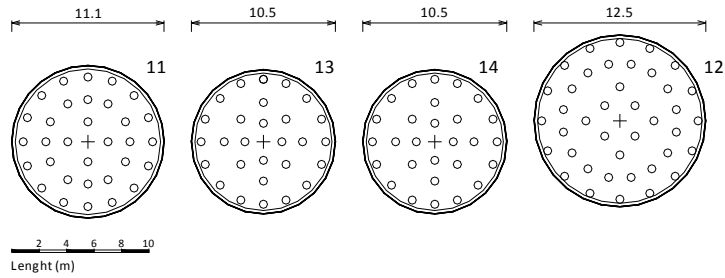


~ 60% less piles

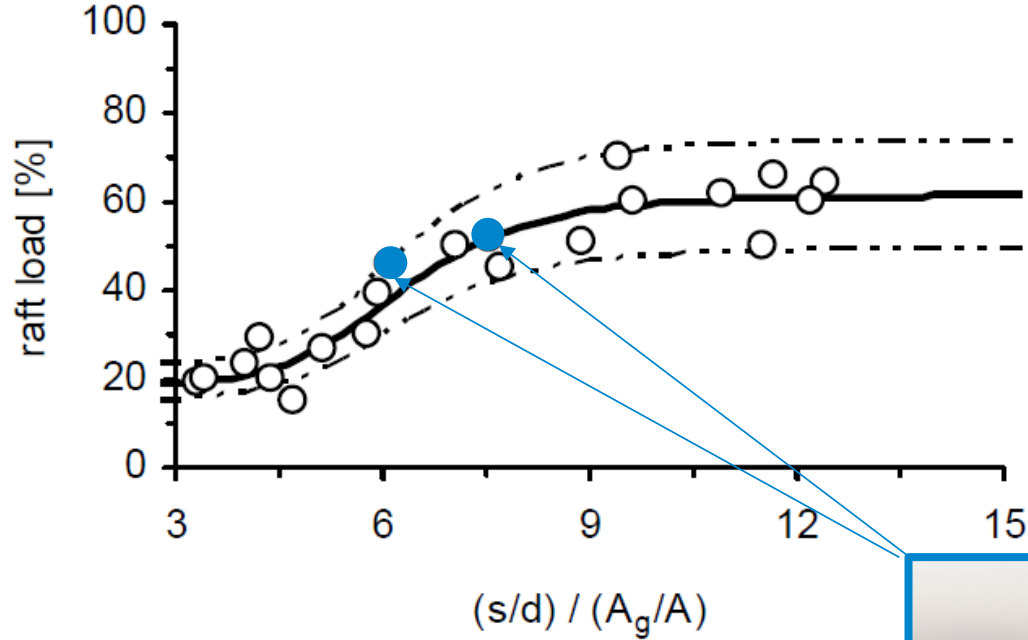
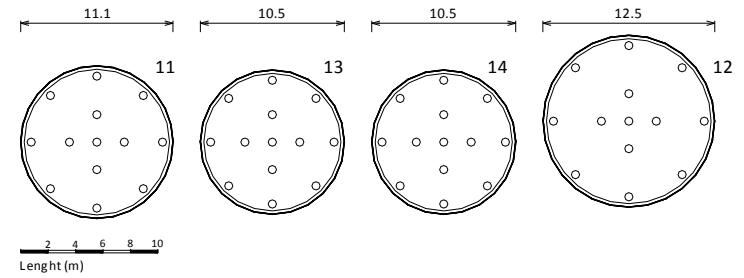
**SATISFACTORY  
PERFORMANCE**



## Original CBD design: 128 piles



## New SBD design: 52 piles





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**Needless to say, more demanding the design is, more efforts should be made in terms of soil investigations (not discussed here).**



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**NO OR LIMITED KNOWLEDGE OF  
THE SUBSOIL, NO RIGHT TO SPEAK  
(NOT ONLY OF PILED RAFT .....)**



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## CONCLUDING REMARKS

- The **variety** of possible situation is such that any **generalisation** is **difficult**





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## CONCLUDING REMARKS

- The **variety** of possible situation is such that any **generalisation** is **difficult**
- Referring to **simple and schematic situation** helped to understand the **great potential** is now available for **significant savings** in the field of piled foundations





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## CONCLUDING REMARKS

- The **variety** of possible situation is such that any **generalisation** is **difficult**
- Referring to **simple and schematic situation** helped to understand the **great potential** is now available for **significant savings** in the field of piled foundations
- The availability of **simple and reliable methods** of analysis makes **possible and relatively easy** the **search for an optimum** solution in each particular case







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Nicht ist so **praktisch**  
wie eine gute **theorie!**

Kurt Lewin, 1946



*“Nothing is more **practical** than a good **theory**”*



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# **Rainer, Mario, Alessandro & Bengt, (known as The Fantastic Four) at Mario's place**

**27/04/2015**



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